

Super-Node SLP: Optimized Vectorization for Code Sequences Containing Operators and Their Inverse Elements

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THE UNIVERSITY of EDINBURGH
informatics





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- Run SLP after the Loop Vectorizer

SLP compared to Loop Vectorization

- Vectorizes across instructions, *NOT* iterations

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for (i=0; i<N; i+=4)
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Loop Vectorization (LV) with VF = 4

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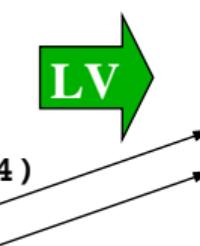
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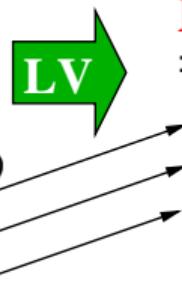
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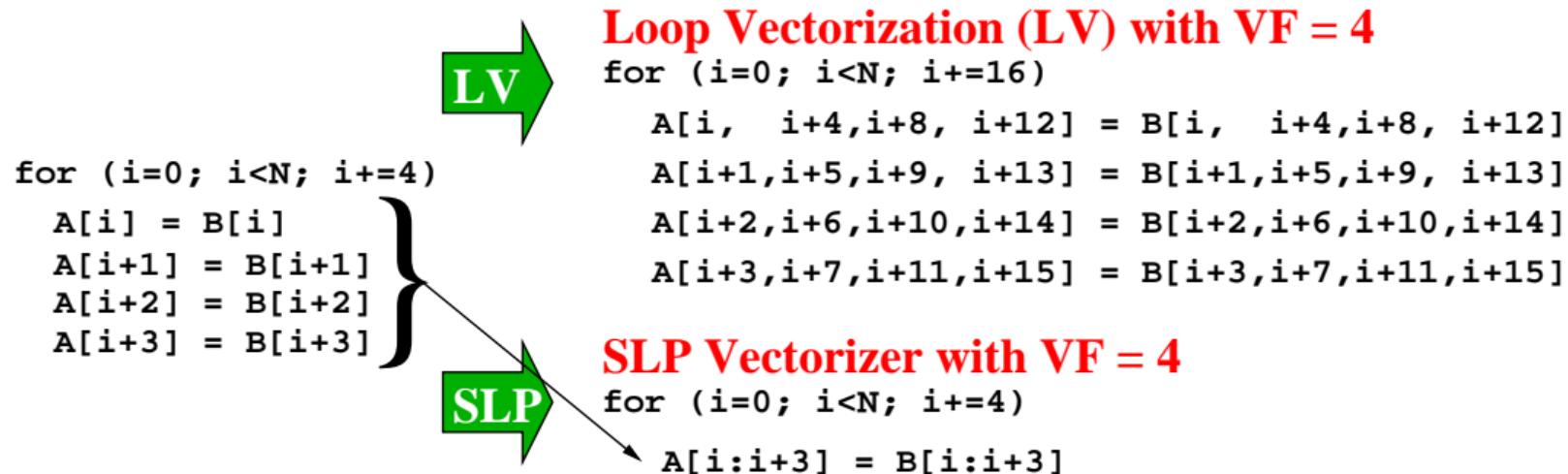


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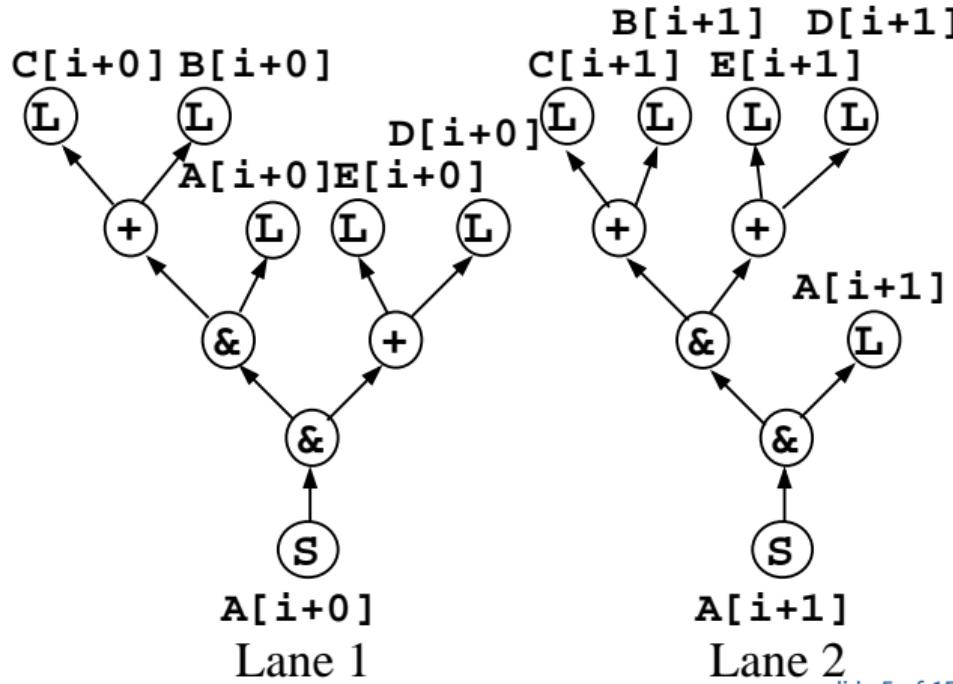


State-of-the-art [Look-Ahead SLP CGO'18]

- Form Multi-Nodes and reorder operands with Look-Ahead heuristic

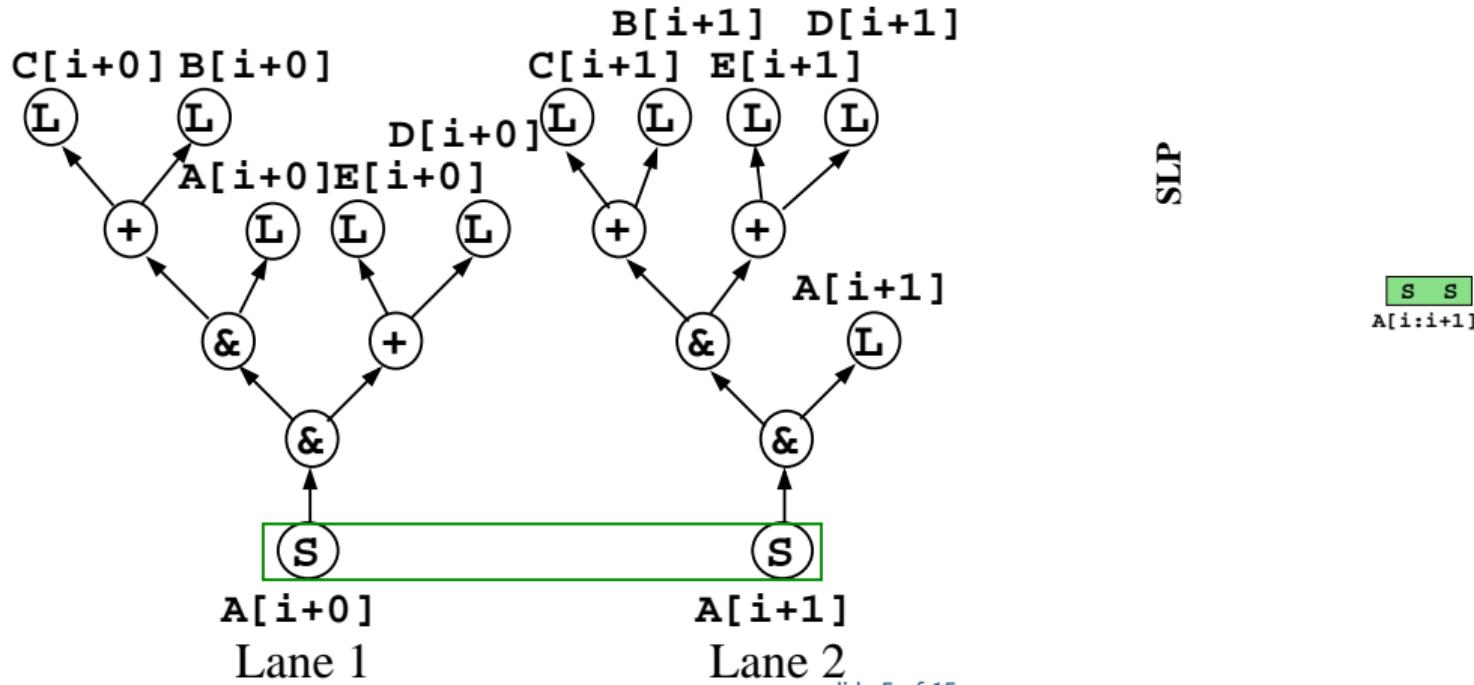
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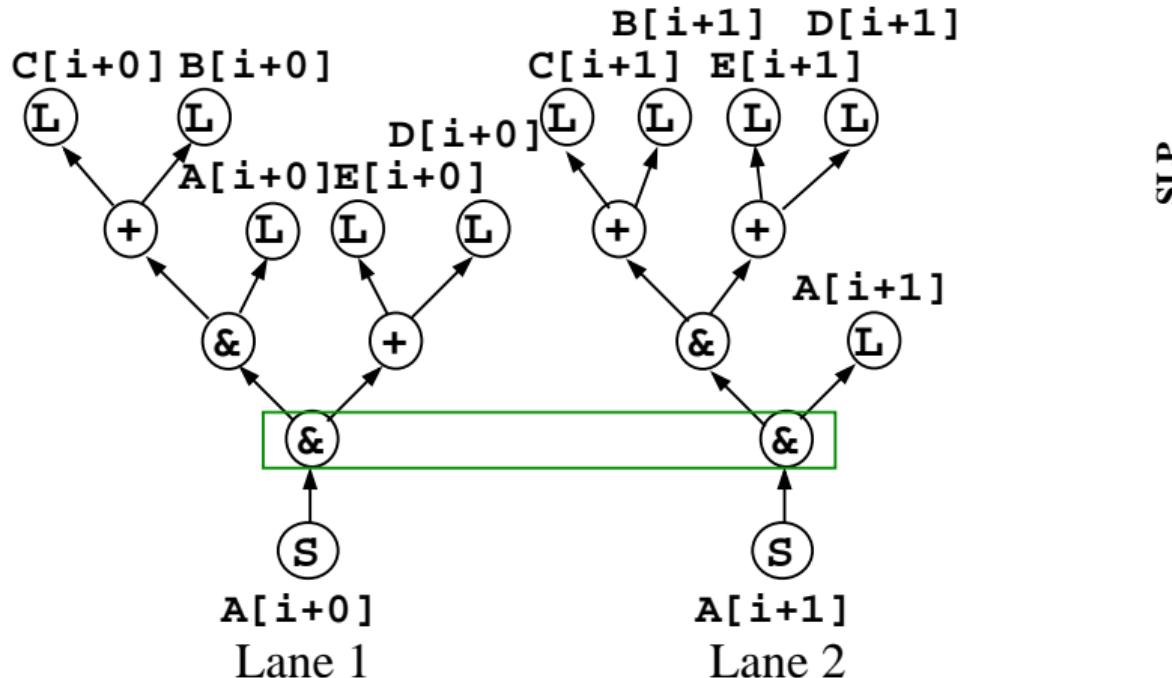
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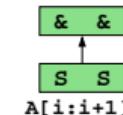


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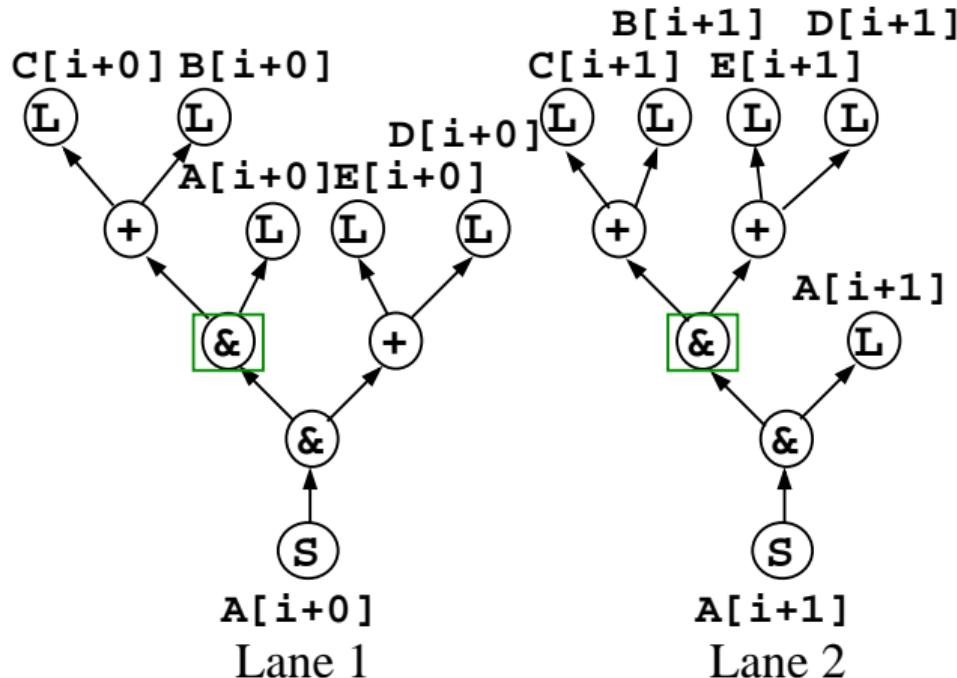


SLP

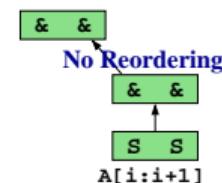


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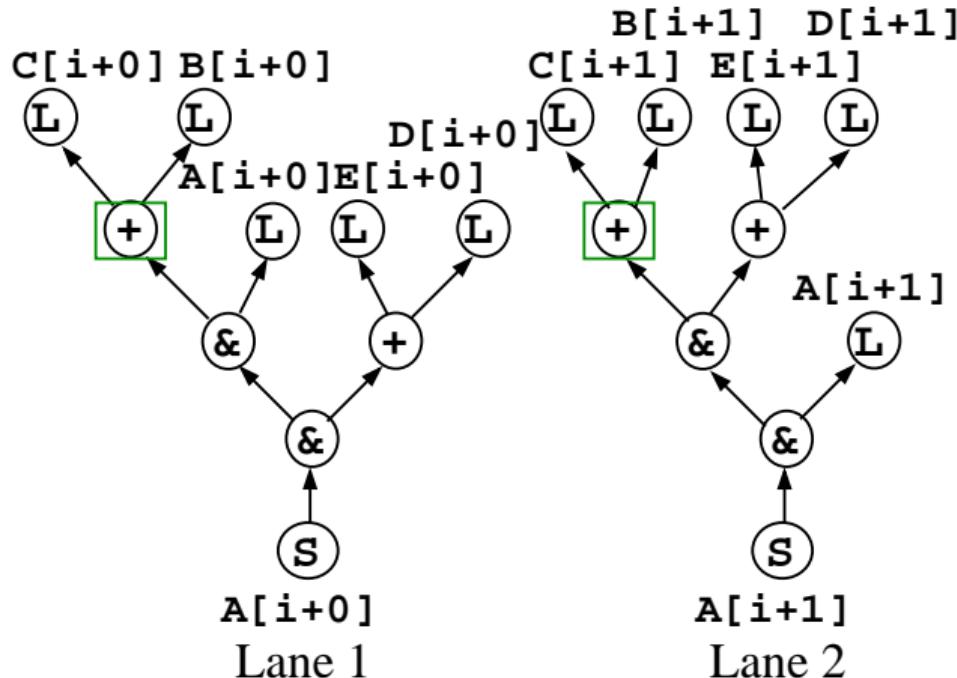


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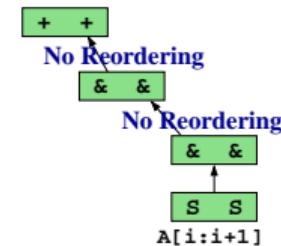


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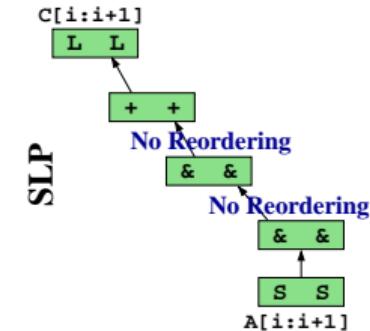
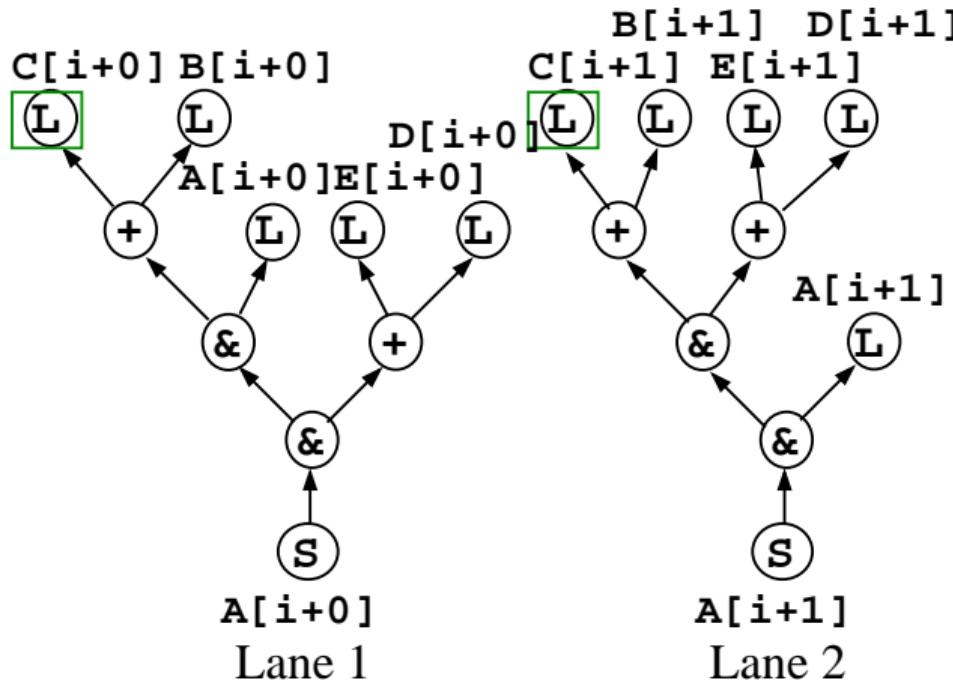


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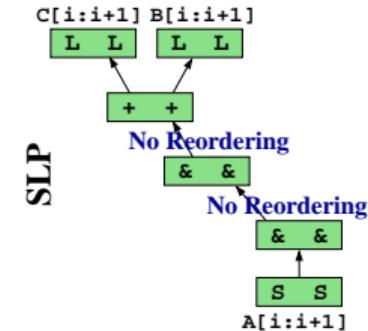
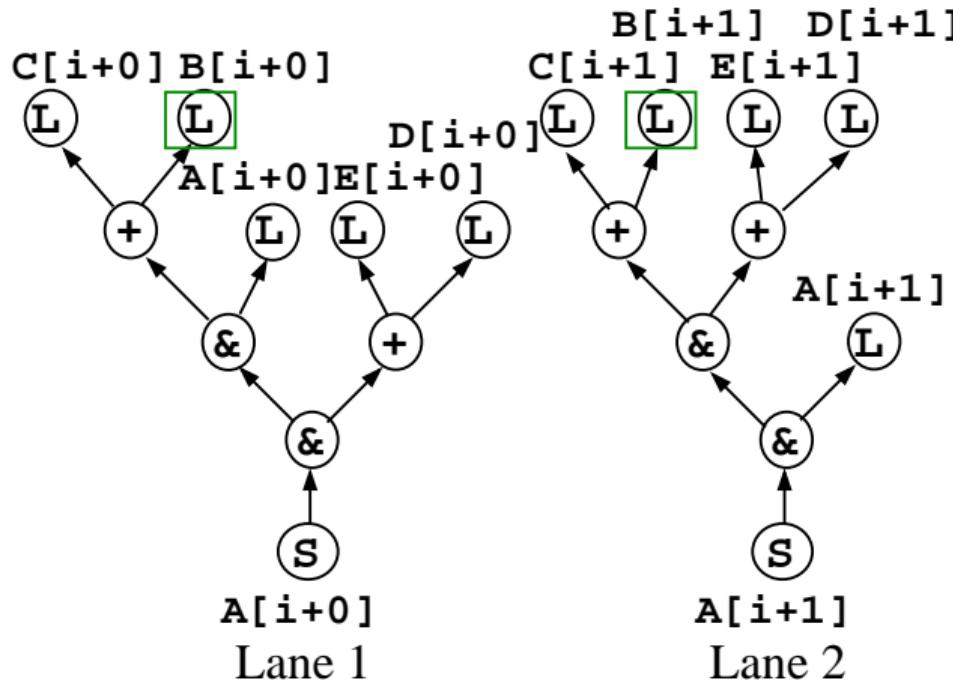
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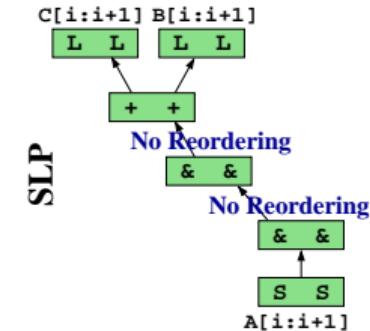
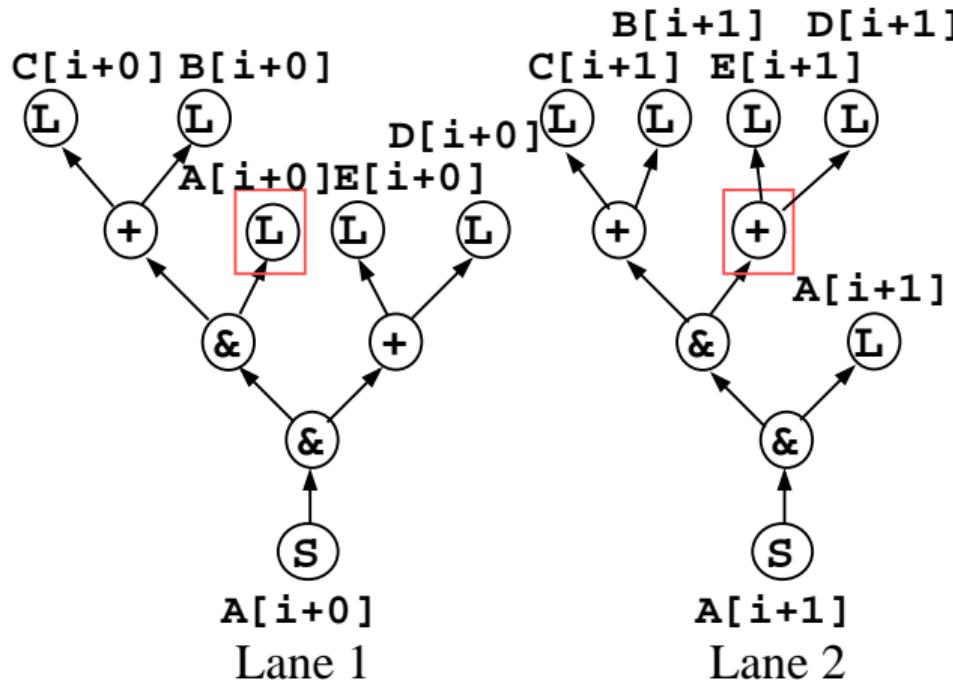
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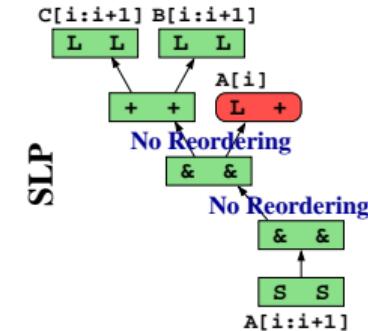
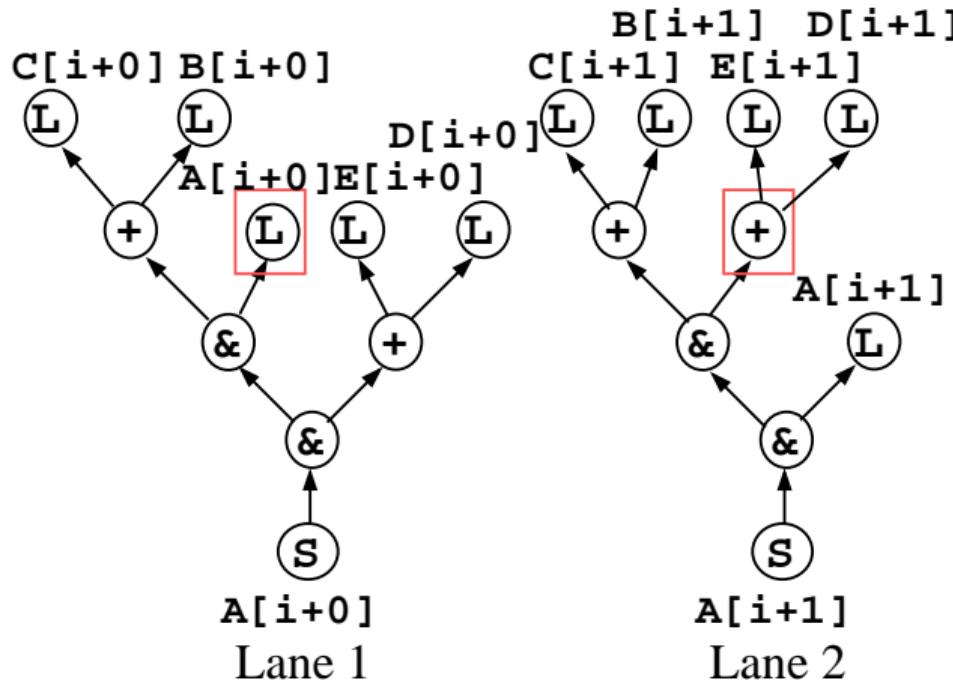
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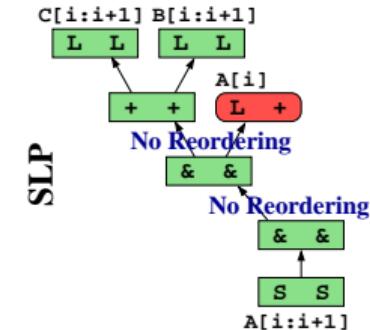
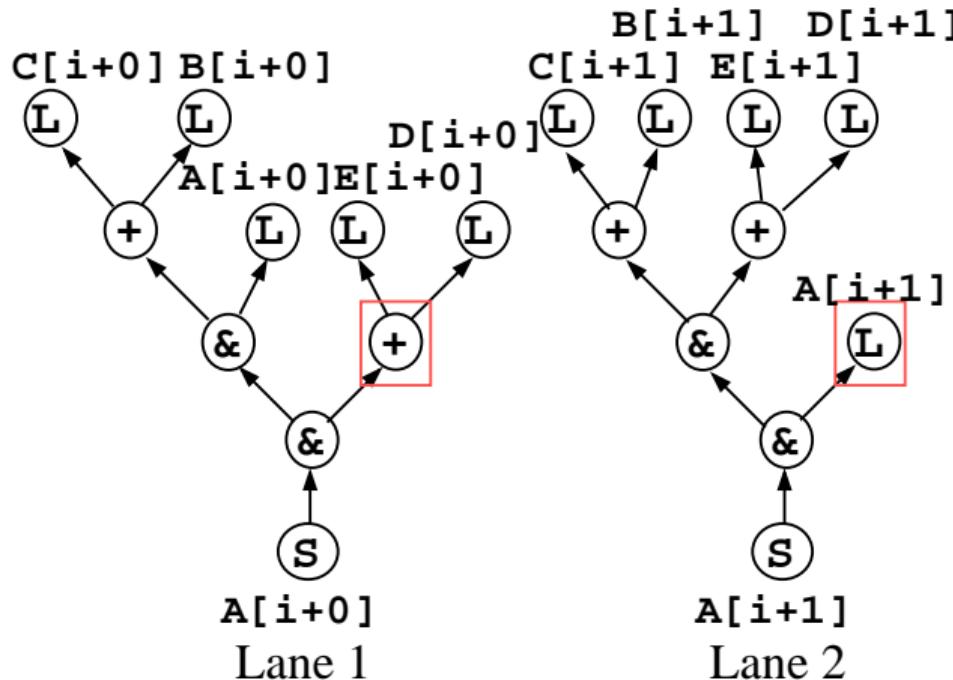
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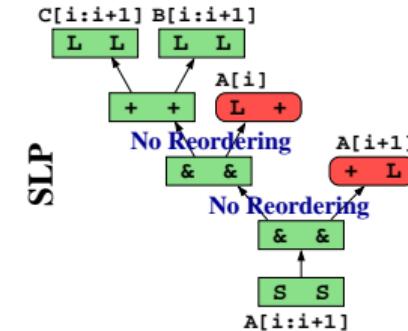
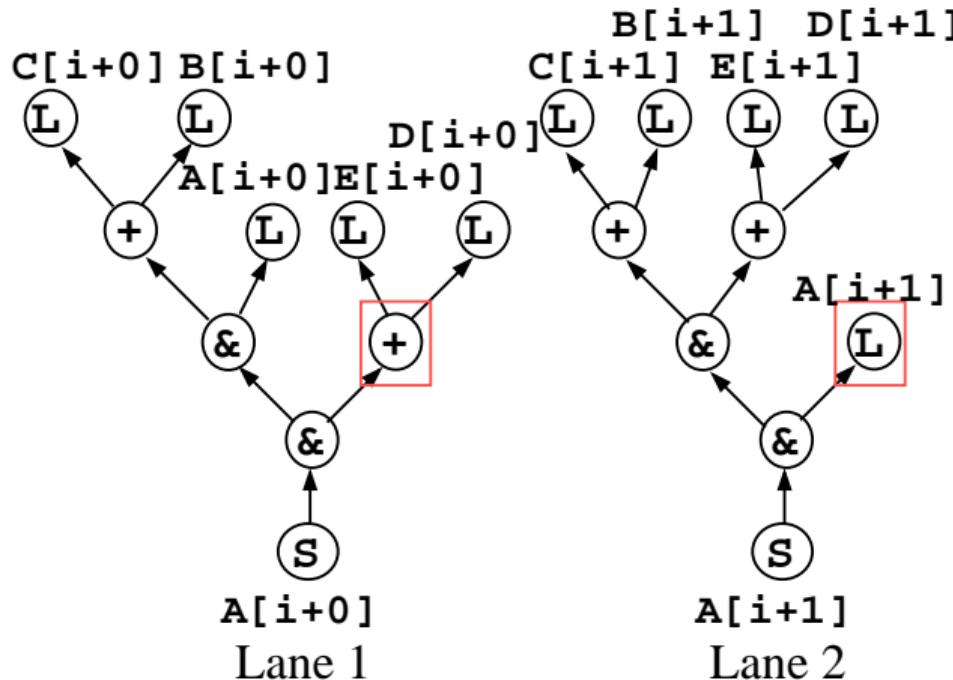
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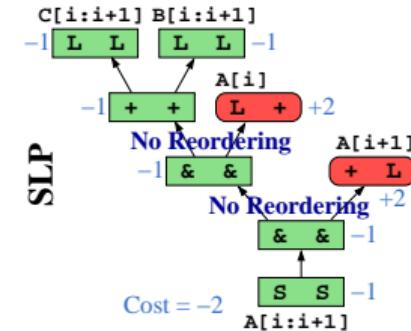
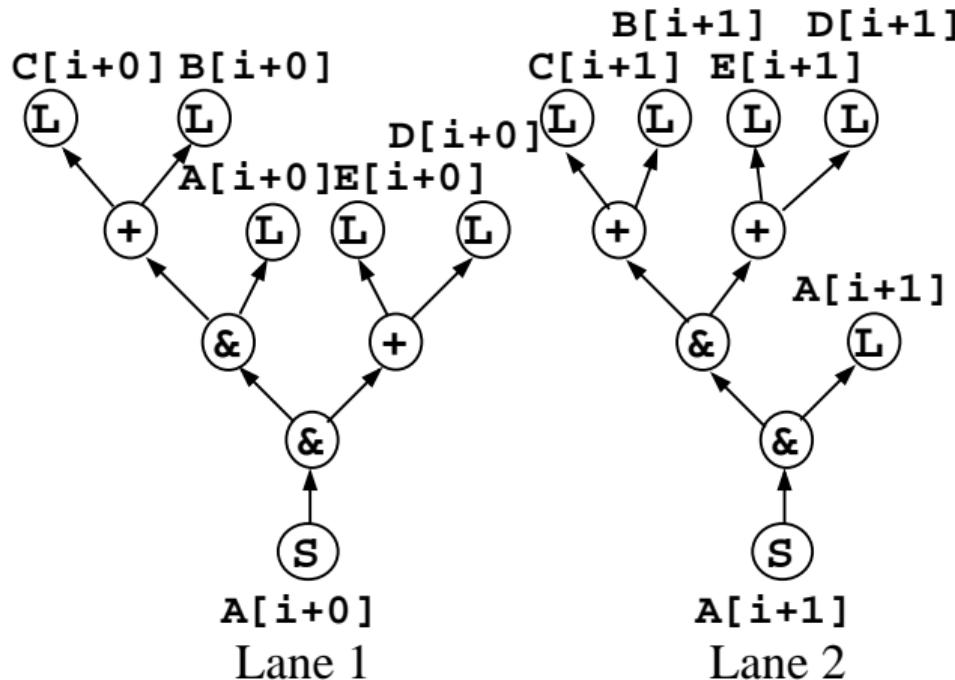
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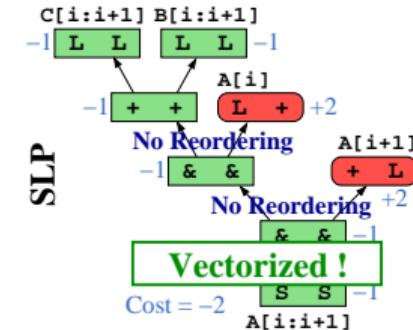
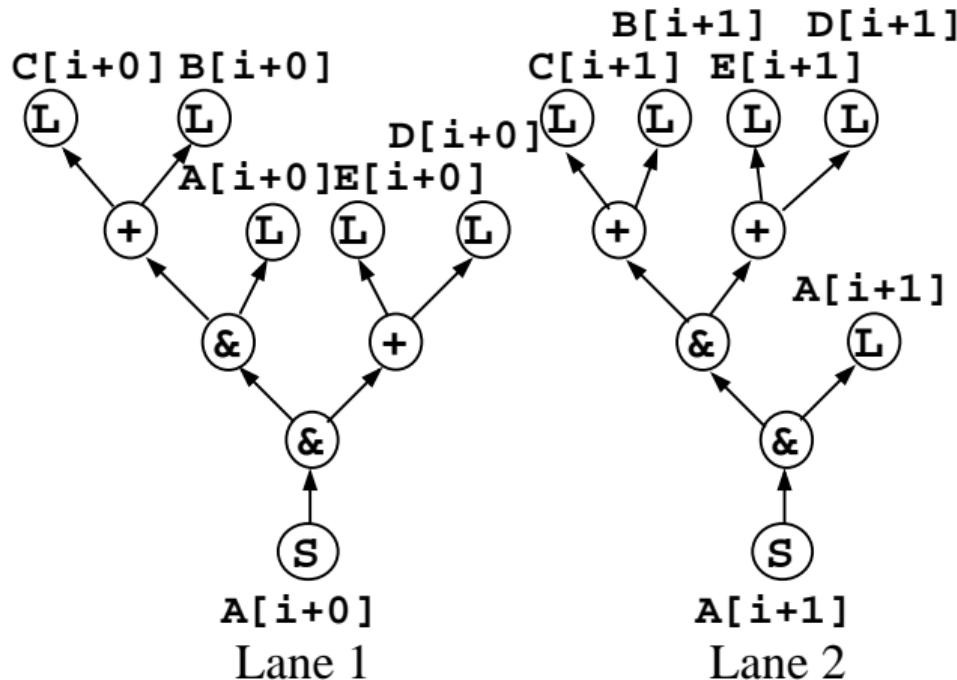
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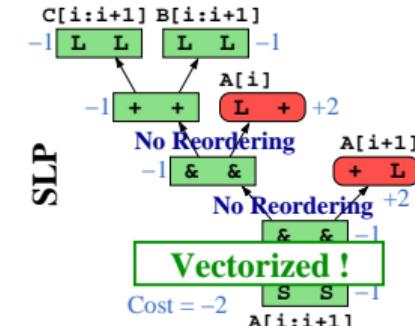
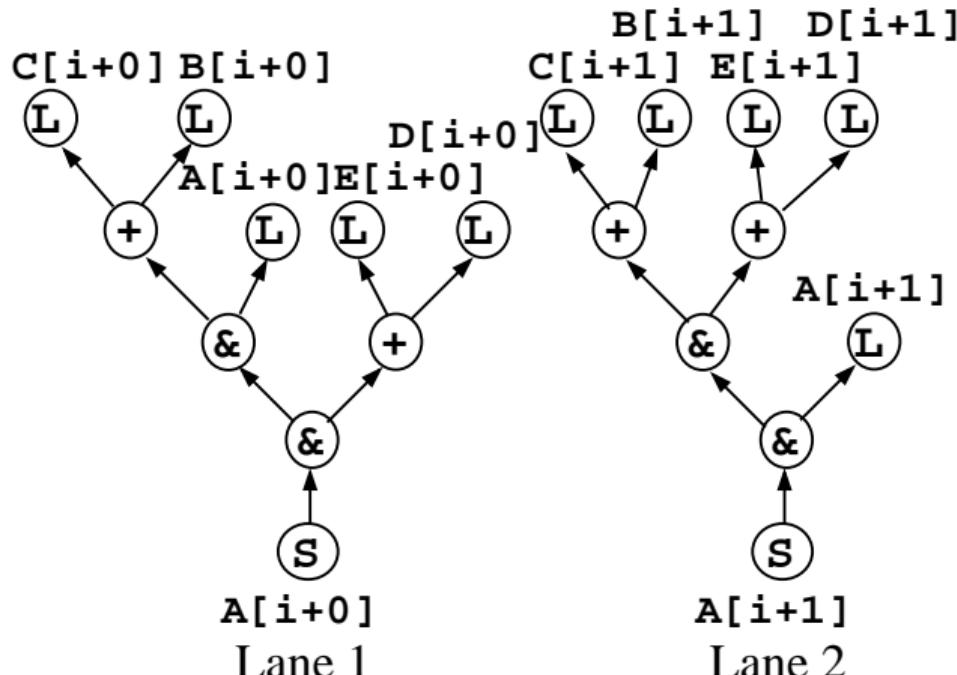
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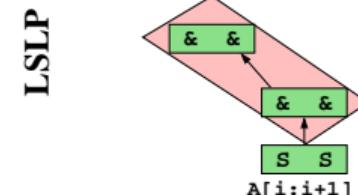
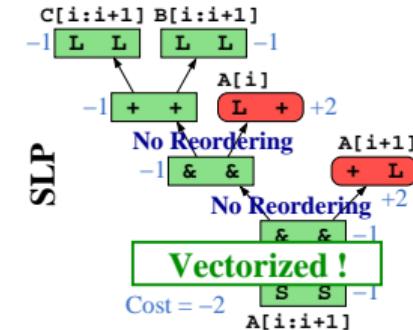
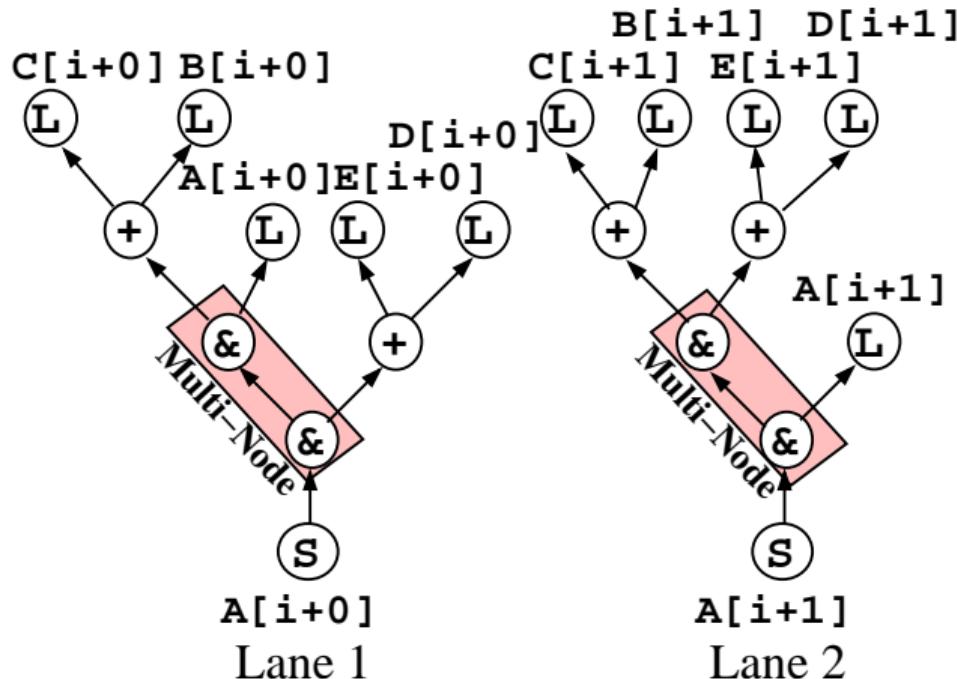
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LSLP

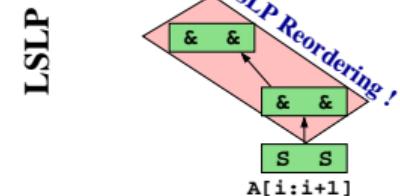
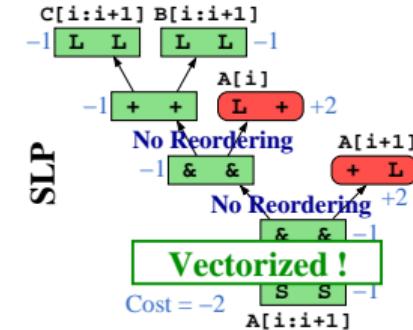
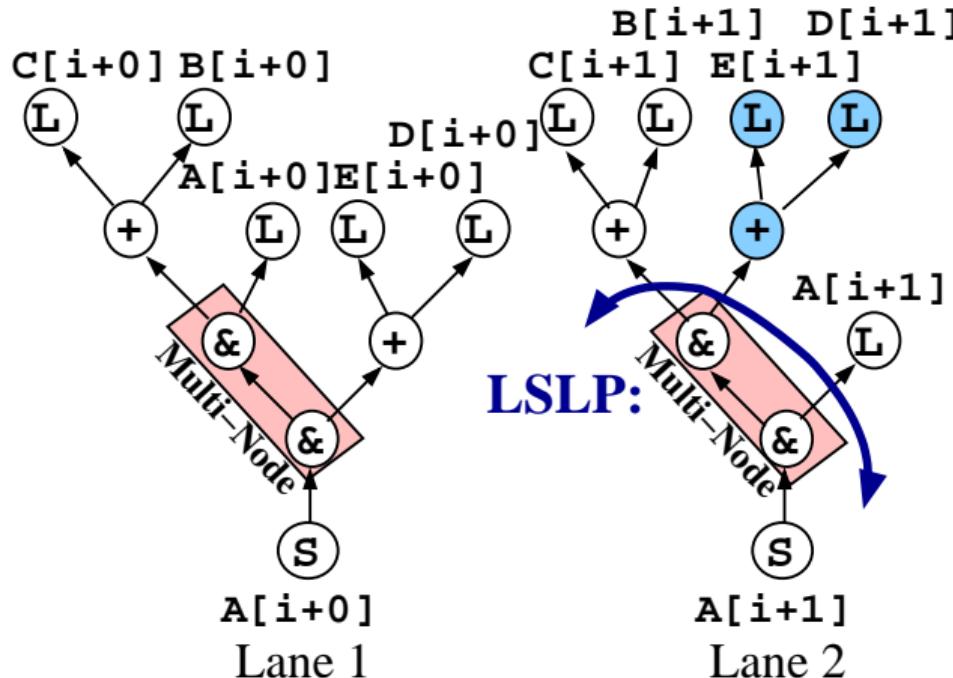
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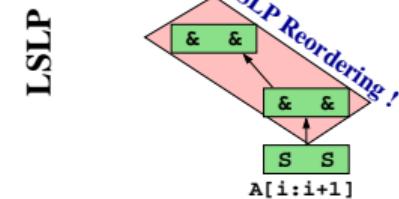
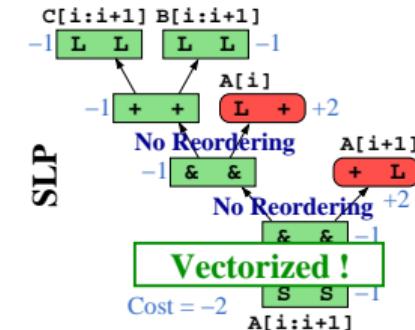
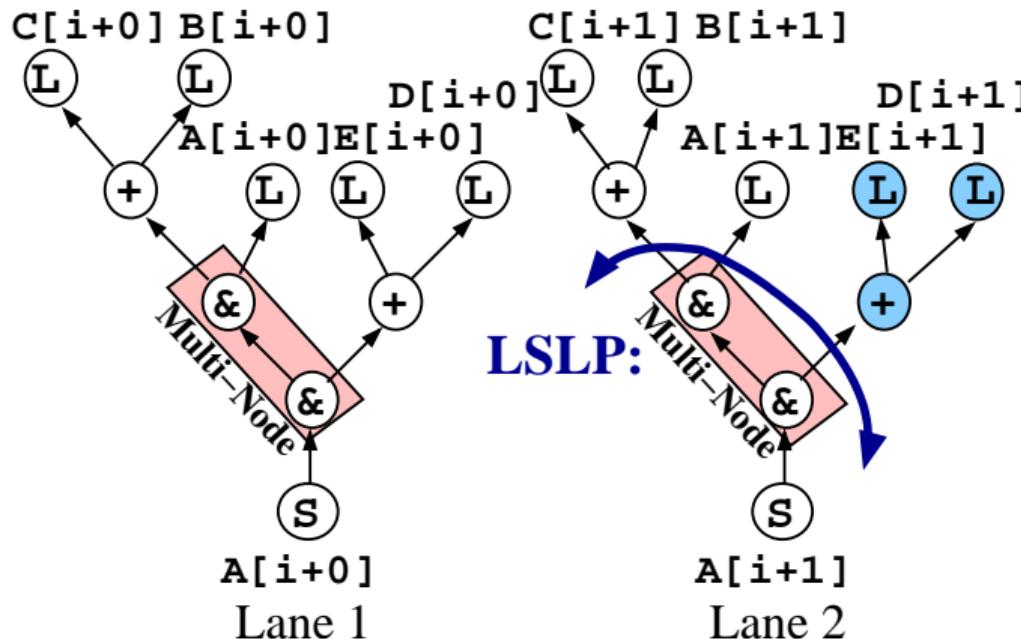
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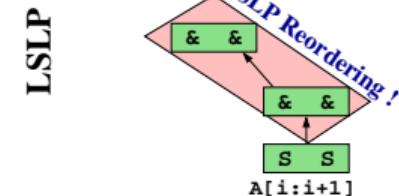
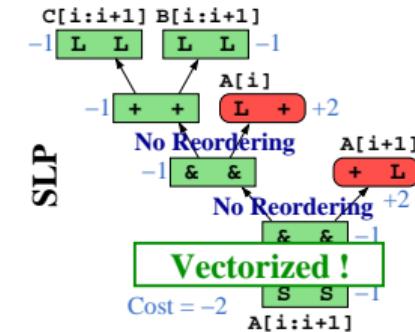
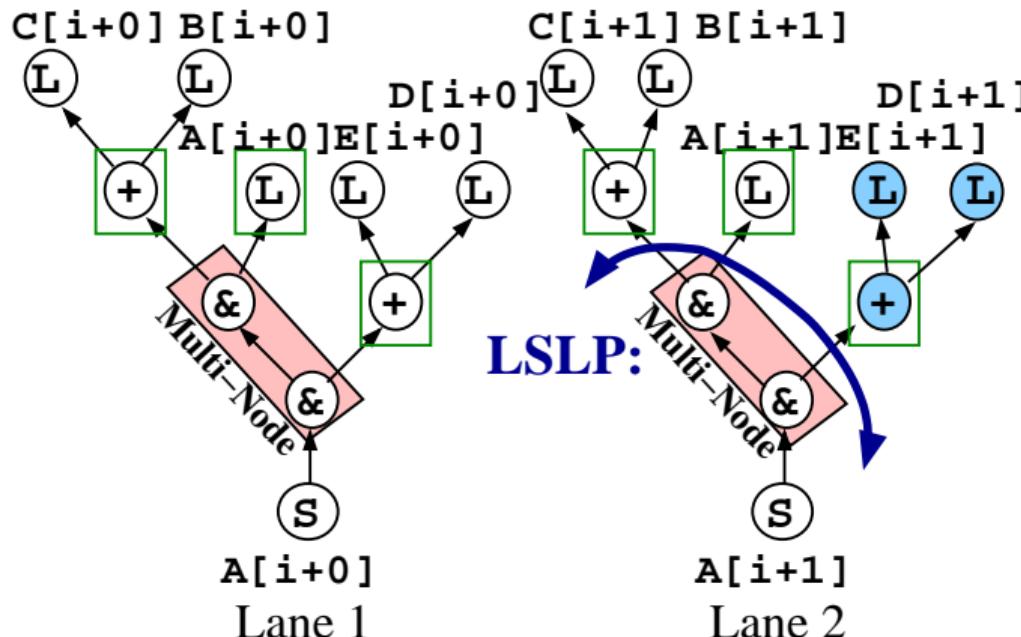
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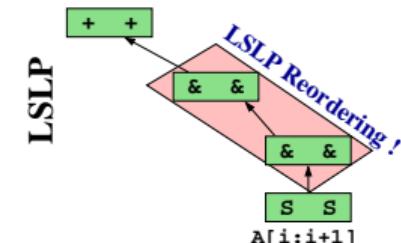
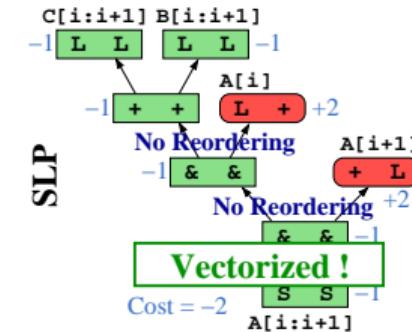
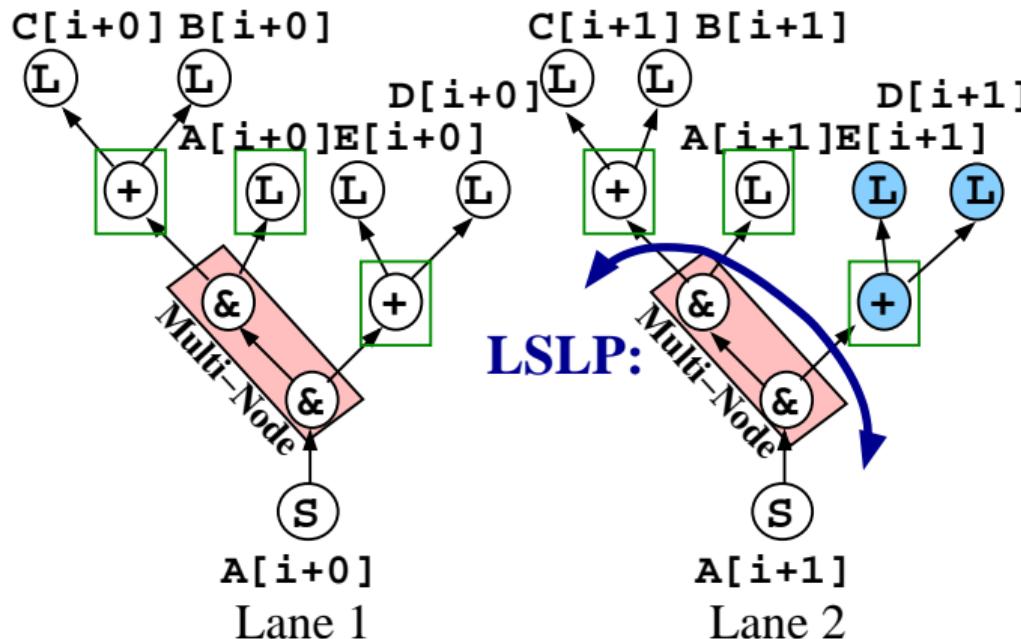
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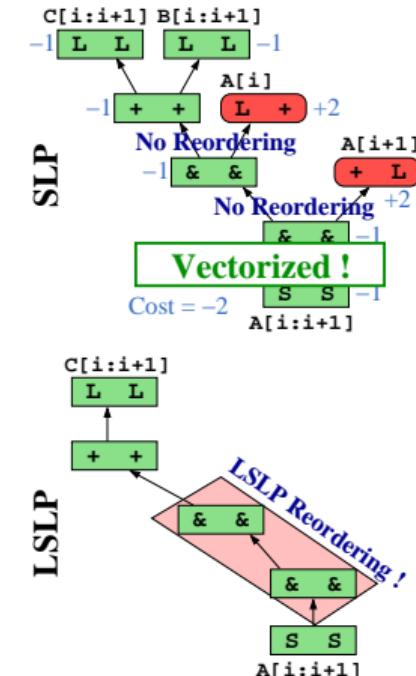
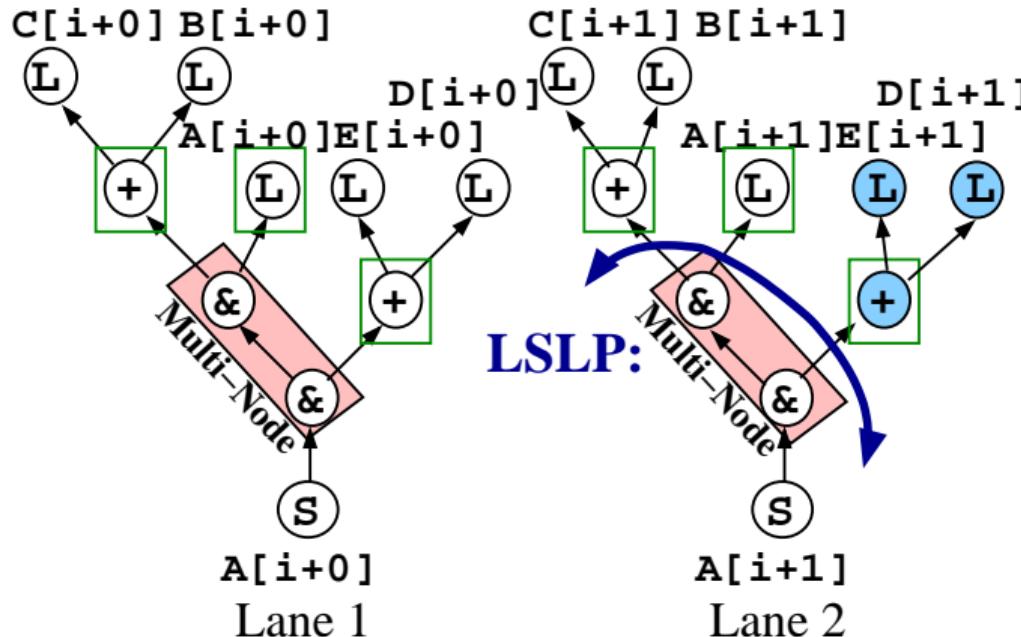
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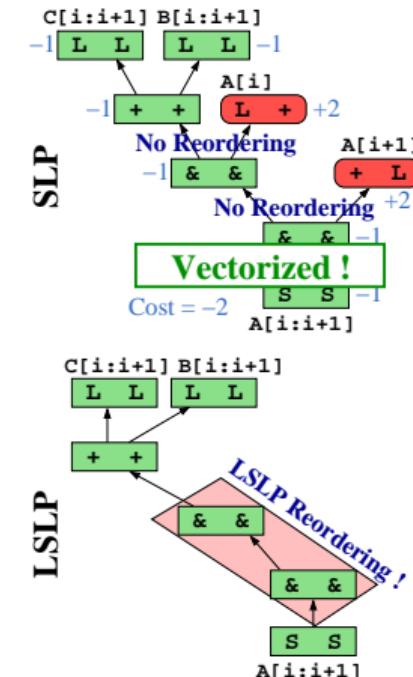
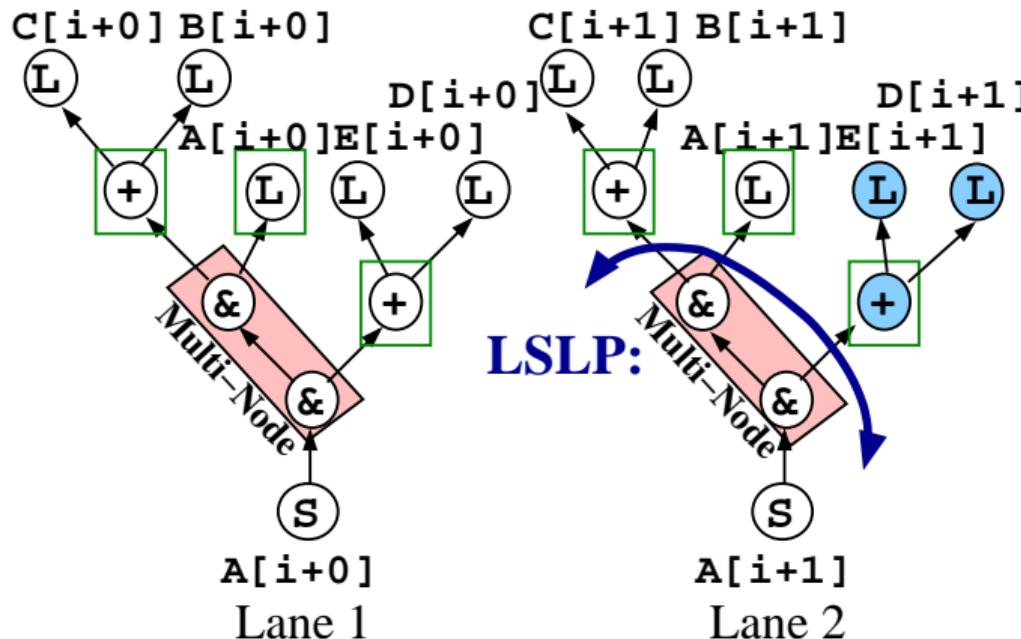
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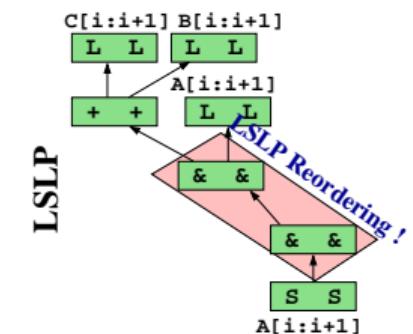
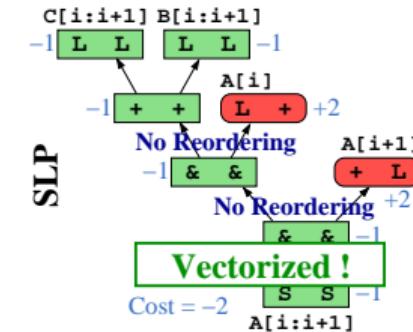
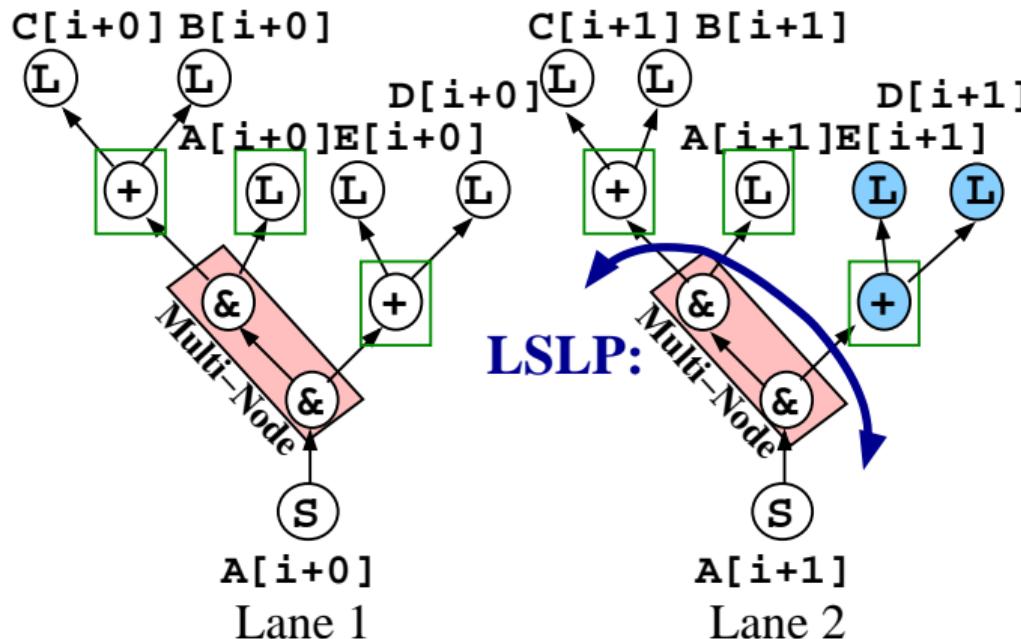
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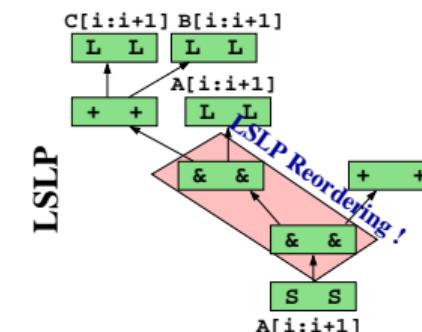
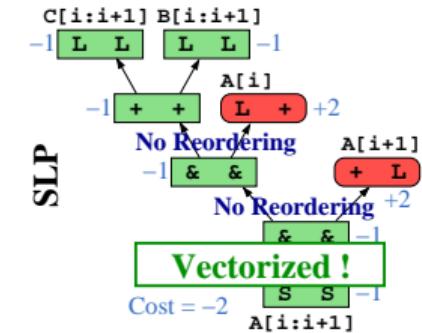
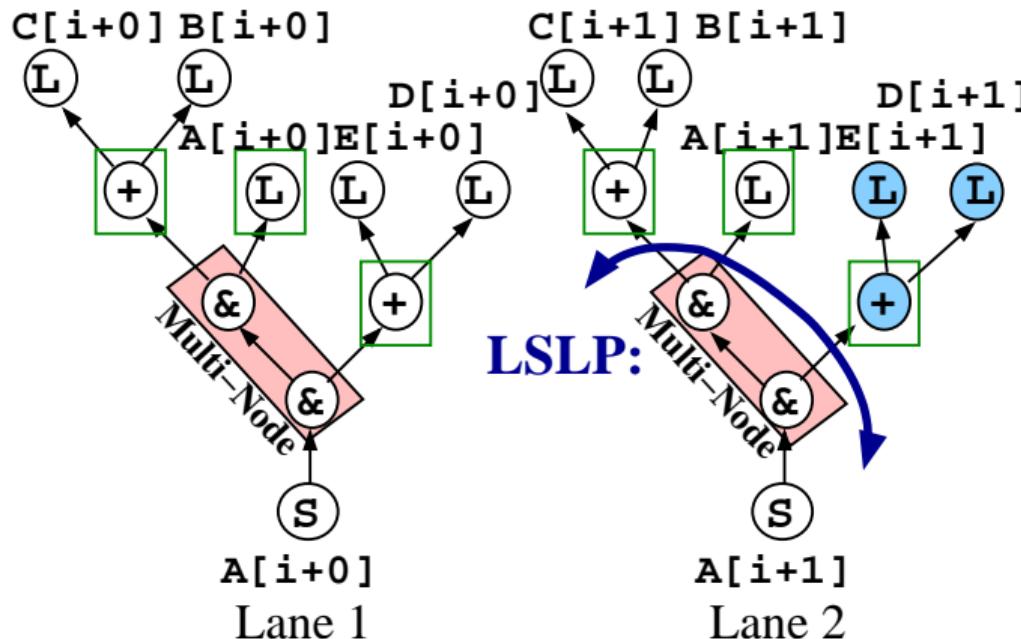
State-of-the-art [Look-Ahead SLP CGO'18]

- Form Multi-Nodes and reorder operands with Look-Ahead heuristic



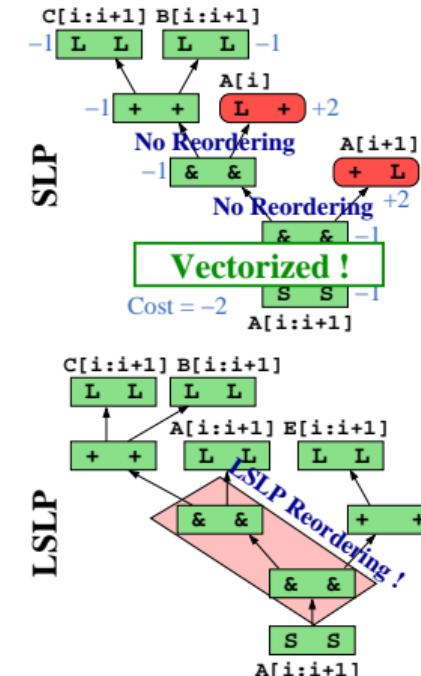
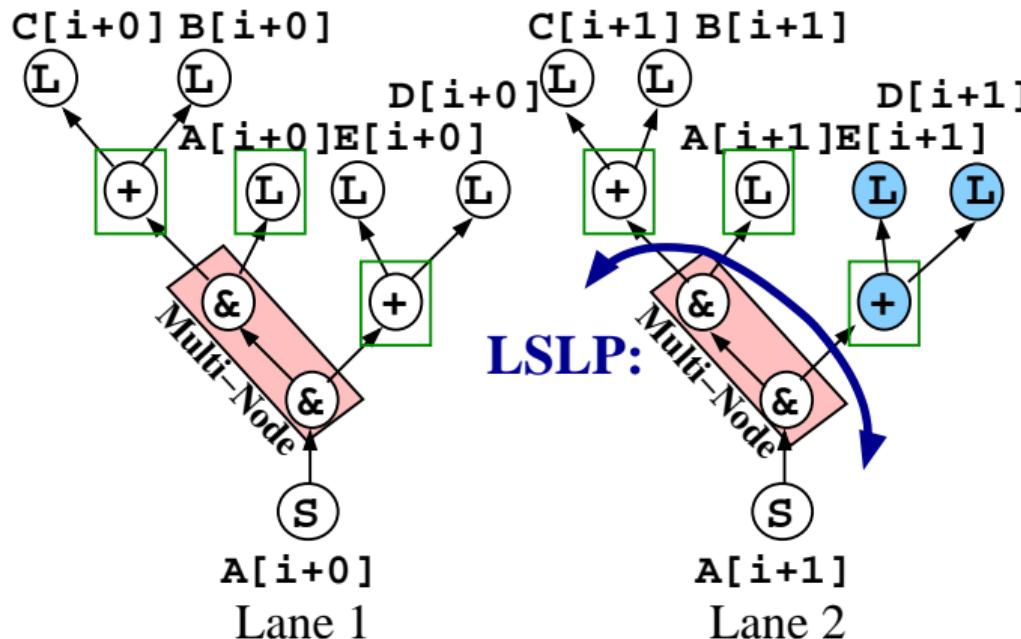
State-of-the-art [Look-Ahead SLP CGO'18]

- Form Multi-Nodes and reorder operands with Look-Ahead heuristic



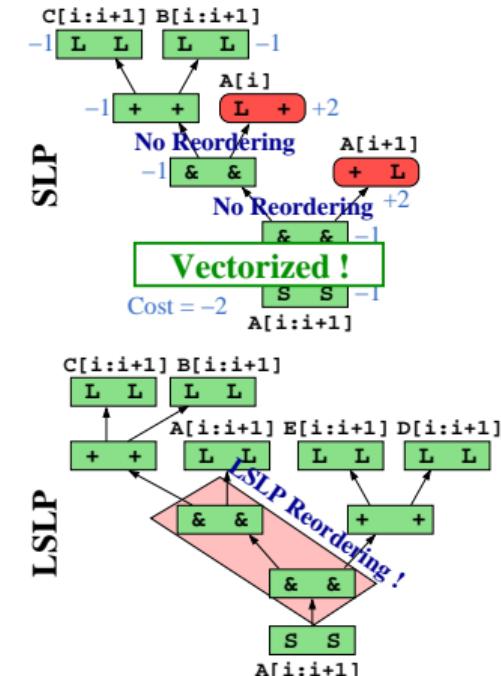
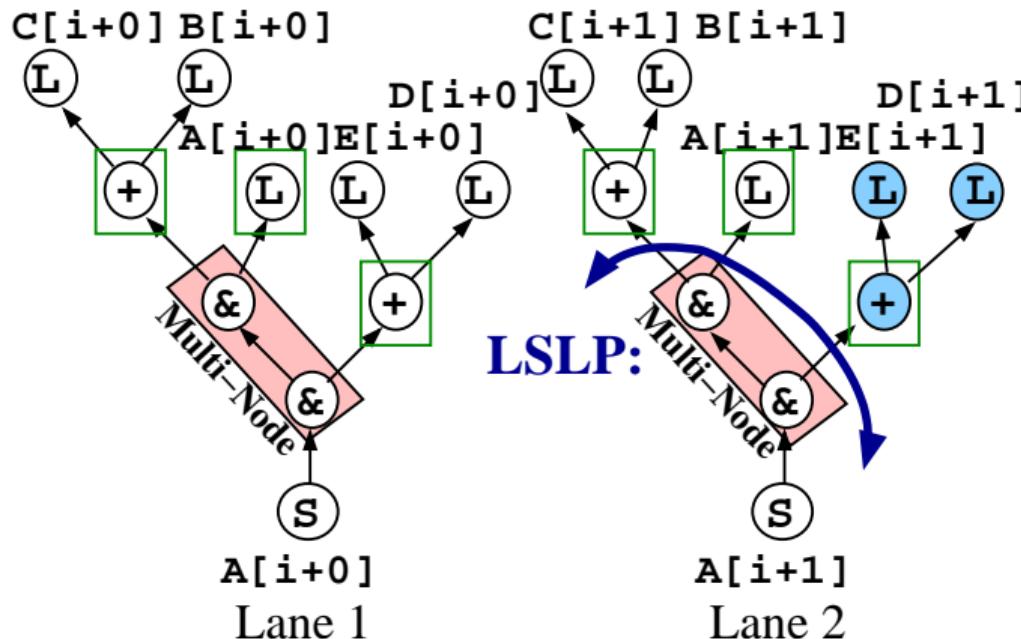
State-of-the-art [Look-Ahead SLP CGO'18]

- Form Multi-Nodes and reorder operands with Look-Ahead heuristic



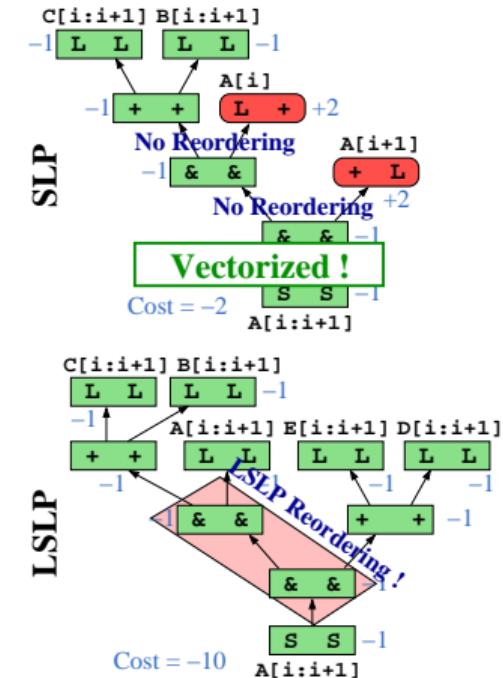
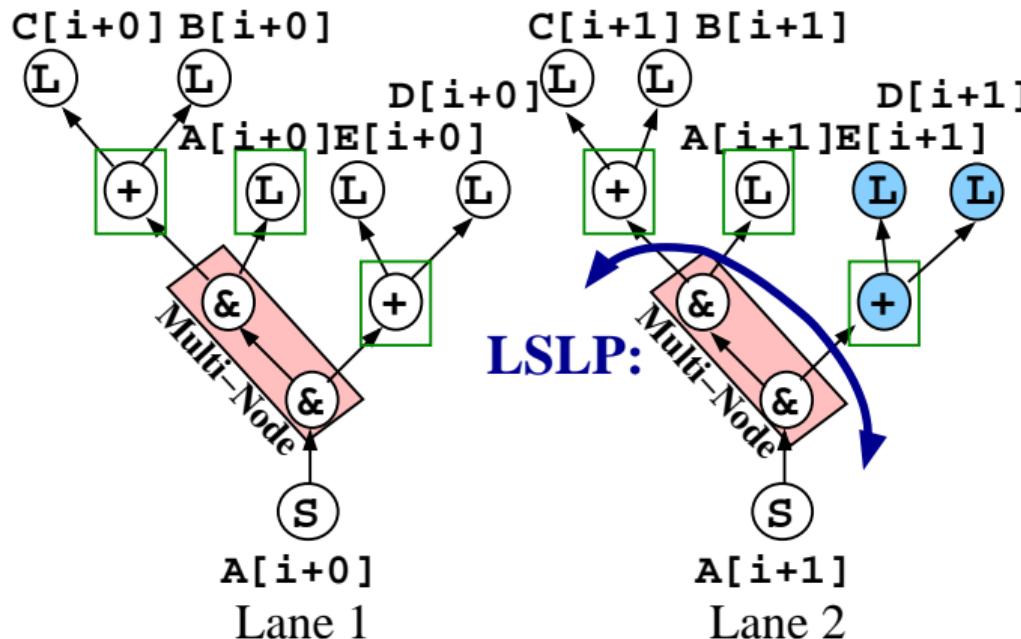
State-of-the-art [Look-Ahead SLP CGO'18]

- Form Multi-Nodes and reorder operands with Look-Ahead heuristic



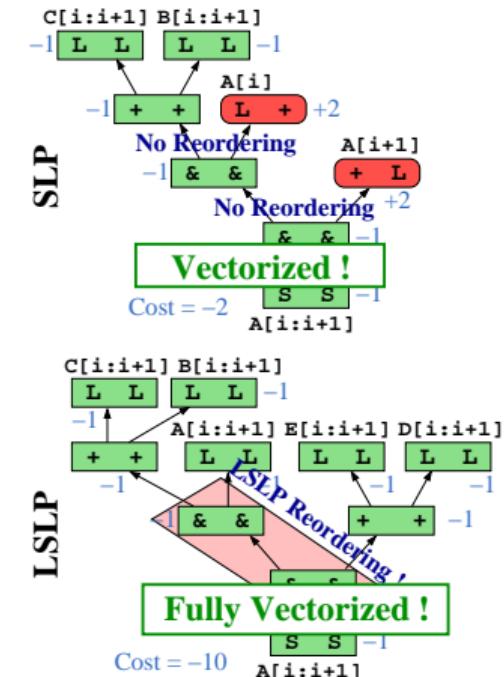
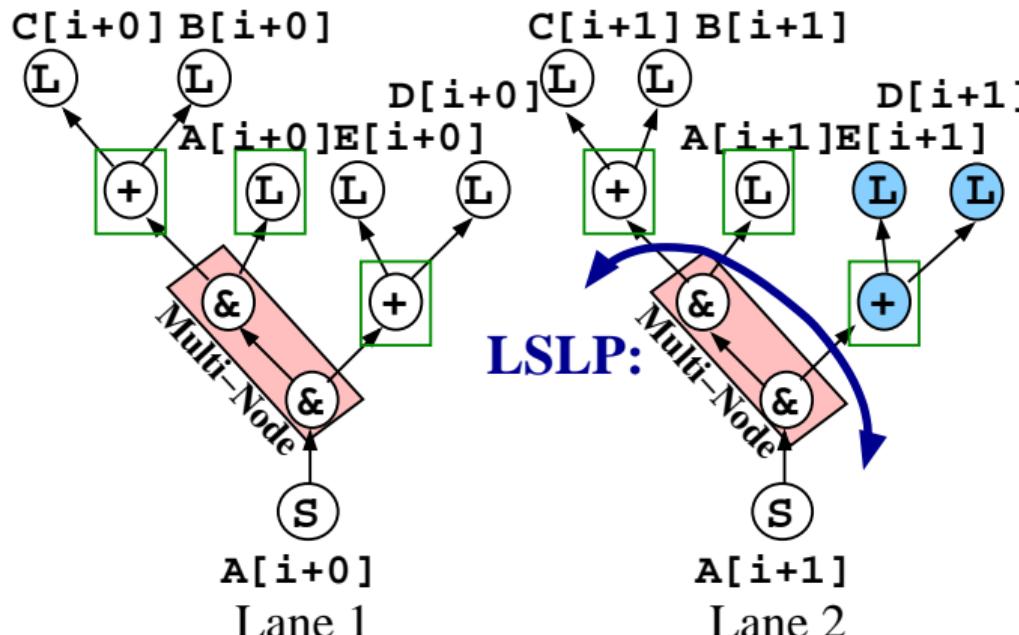
State-of-the-art [Look-Ahead SLP CGO'18]

- Form Multi-Nodes and reorder operands with Look-Ahead heuristic



State-of-the-art [Look-Ahead SLP CGO'18]

- Form Multi-Nodes and reorder operands with Look-Ahead heuristic



Multi-Node (LSLP) VS Super-Node (SuperNode-SLP)

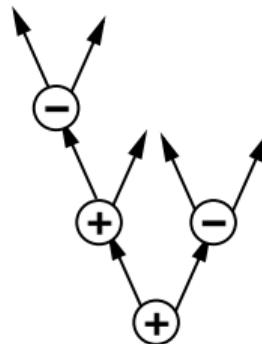
- The inverse element of ADD(+) is SUB(-)

Multi-Node (LSLP) VS Super-Node (SuperNode-SLP)

- The inverse element of ADD(+) is SUB(-)
- Multi-Nodes cannot handle inverse elements

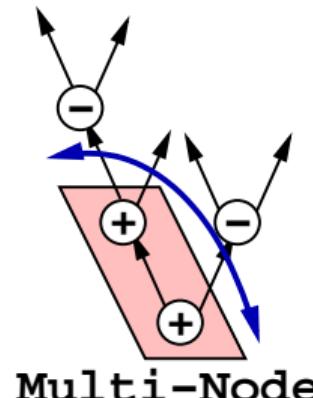
Multi-Node (LSLP) VS Super-Node (SuperNode-SLP)

- The inverse element of ADD(+) is SUB(-)
- Multi-Nodes cannot handle inverse elements



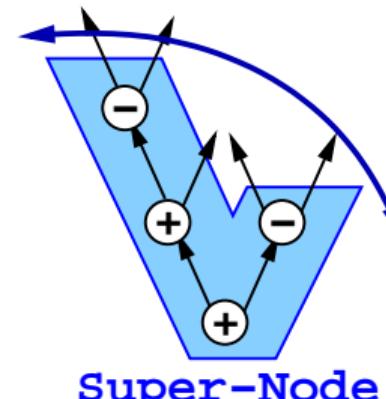
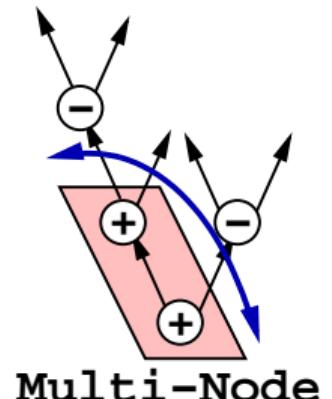
Multi-Node (LSLP) VS Super-Node (SuperNode-SLP)

- The inverse element of ADD(+) is SUB(-)
- Multi-Nodes cannot handle inverse elements



Multi-Node (LSLP) VS Super-Node (SuperNode-SLP)

- The inverse element of ADD(+) is SUB(-)
- Multi-Nodes cannot handle inverse elements
- Super-Nodes **can** reorder across them when legal

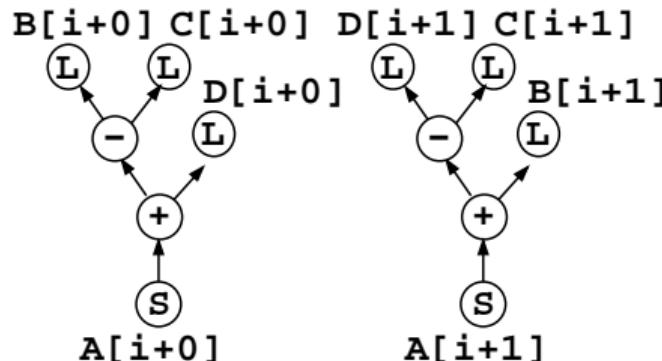


LSLP fails in the presence of inverse elements

```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```

LSLP fails in the presence of inverse elements

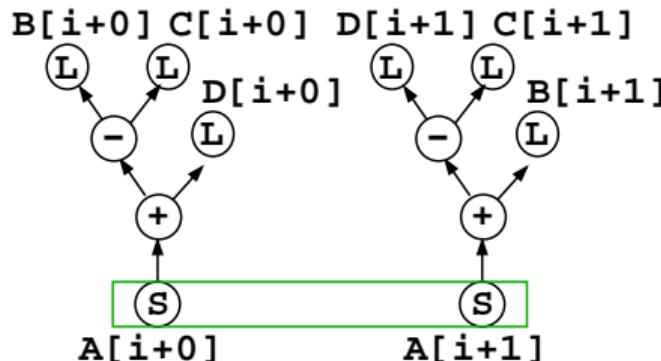
```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```



LSLP fails in the presence of inverse elements

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A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```

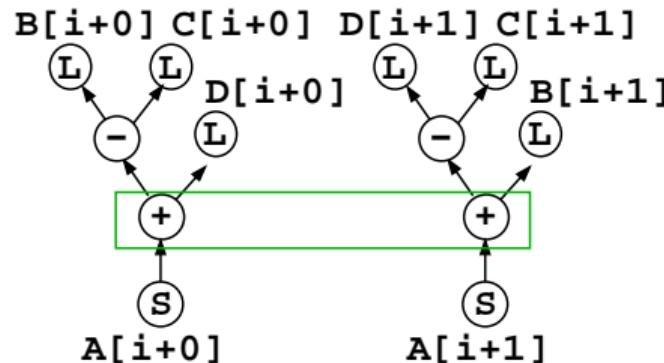
(L) SLP



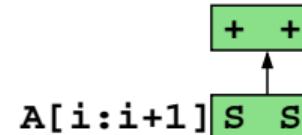
$A[i:i+1] \boxed{S \quad S}$

LSLP fails in the presence of inverse elements

```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```

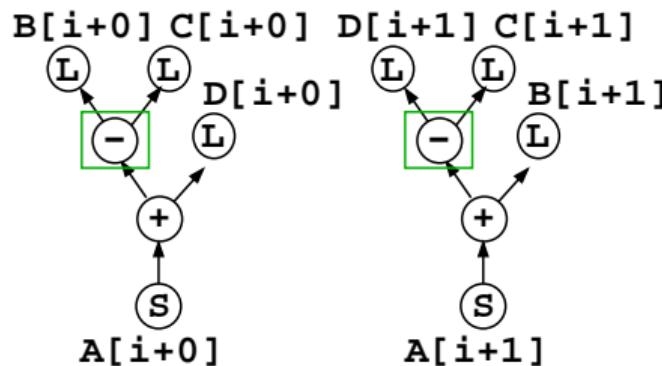


(L) SLP

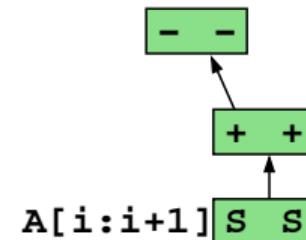


LSLP fails in the presence of inverse elements

```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```

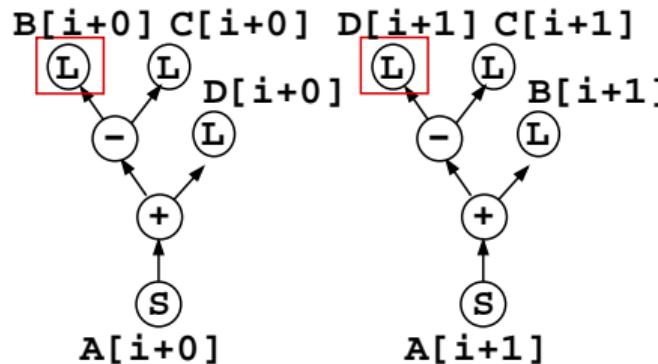


(L) SLP

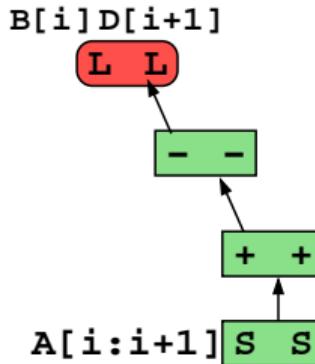


LSLP fails in the presence of inverse elements

```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```

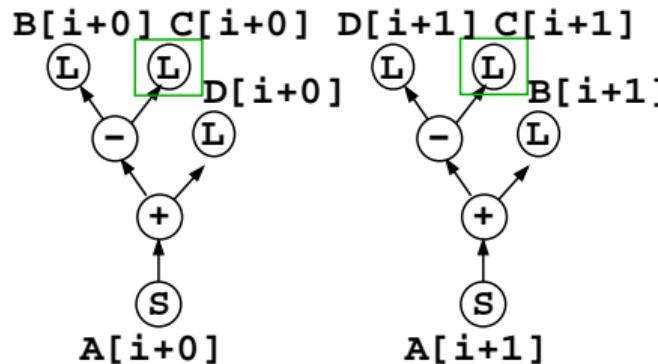


(L) SLP

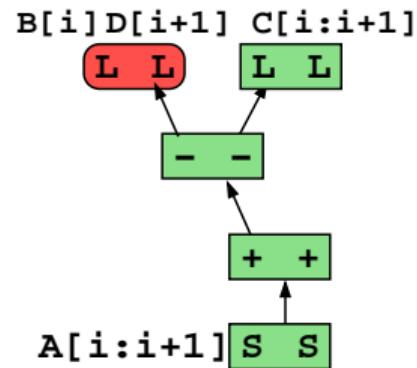


LSLP fails in the presence of inverse elements

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long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```

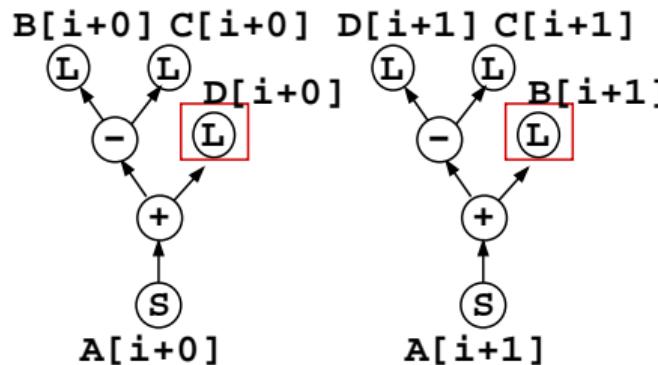


(L) SLP

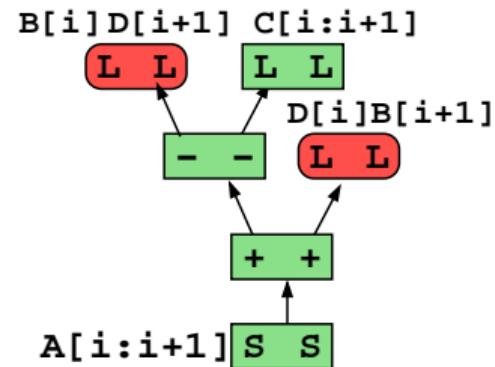


LSLP fails in the presence of inverse elements

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long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```

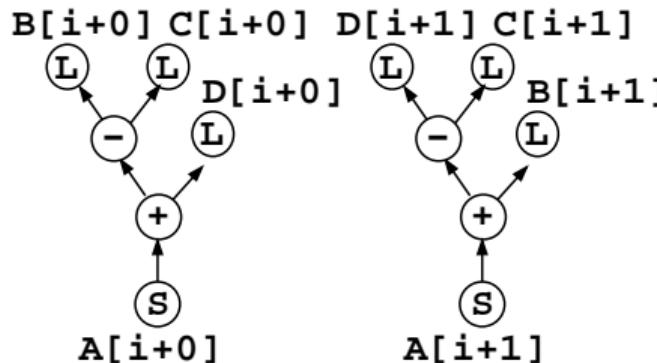


(L) SLP

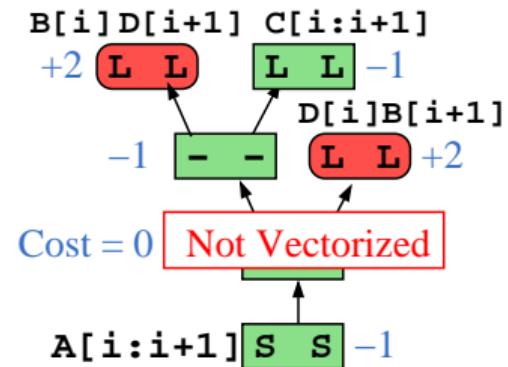


LSLP fails in the presence of inverse elements

```
long A[], B[], C[], D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```

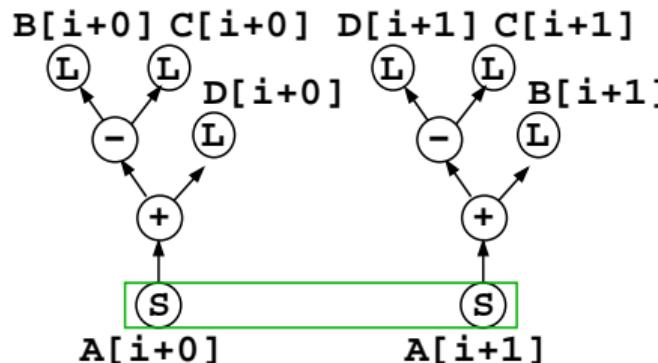


(L) SLP



LSLP fails in the presence of inverse elements

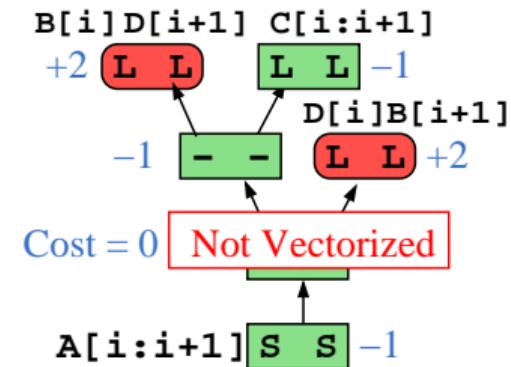
```
long A[], B[], C[], D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```



(L) SLP

SN-SLP

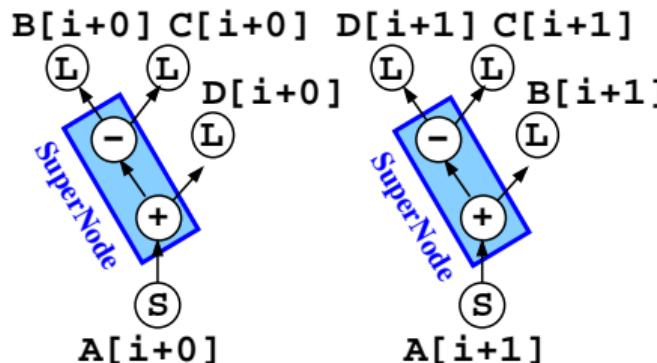
$A[i:i+1] \boxed{S \ S}$



Cost = 0

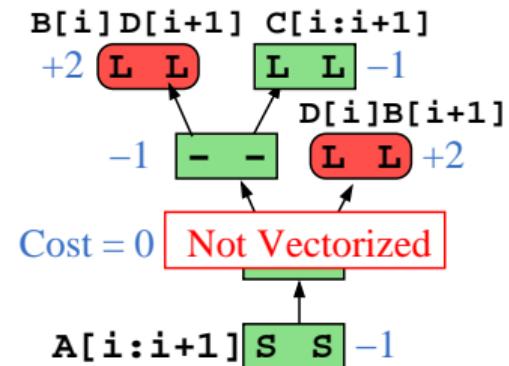
LSLP fails in the presence of inverse elements

```
long A[], B[], C[], D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```



(L) SLP

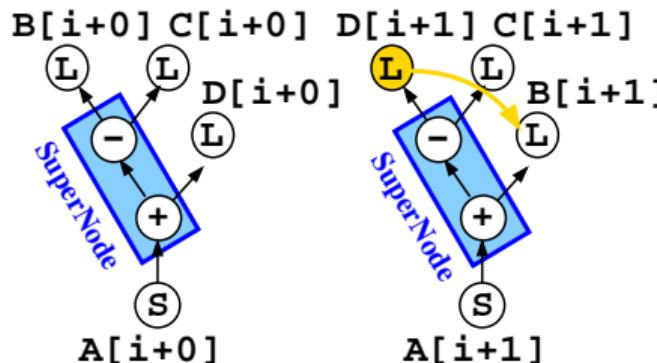
SN-SLP



$A[i:i+1]$ S S

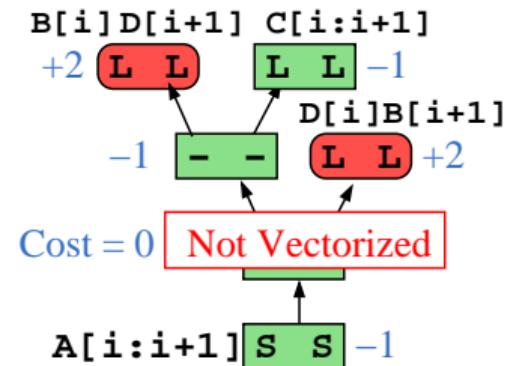
LSLP fails in the presence of inverse elements

```
long A[], B[], C[], D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```



(L) SLP

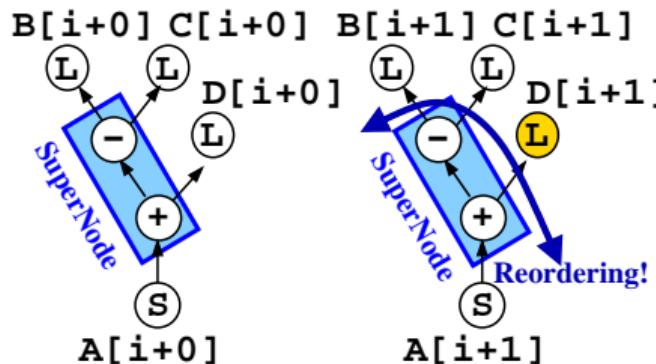
SN-SLP



$A[i:i+1] \boxed{S\ S}$

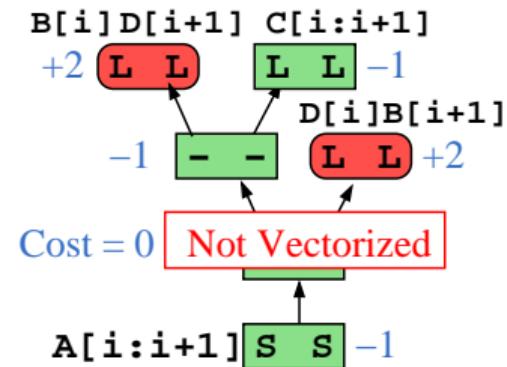
LSLP fails in the presence of inverse elements

```
long A[], B[], C[], D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```



(L) SLP

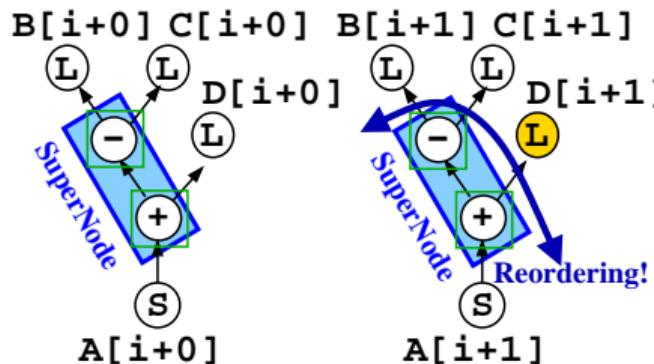
SN-SLP



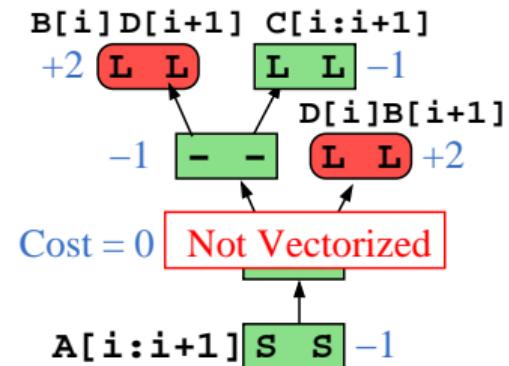
$A[i:i+1]$ **S S**

LSLP fails in the presence of inverse elements

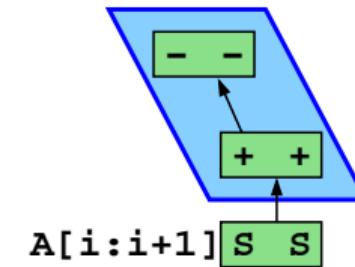
```
long A[], B[], C[], D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```



(L) SLP

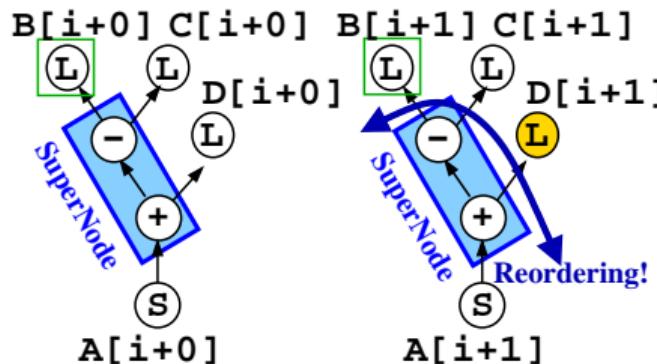


SN-SLP



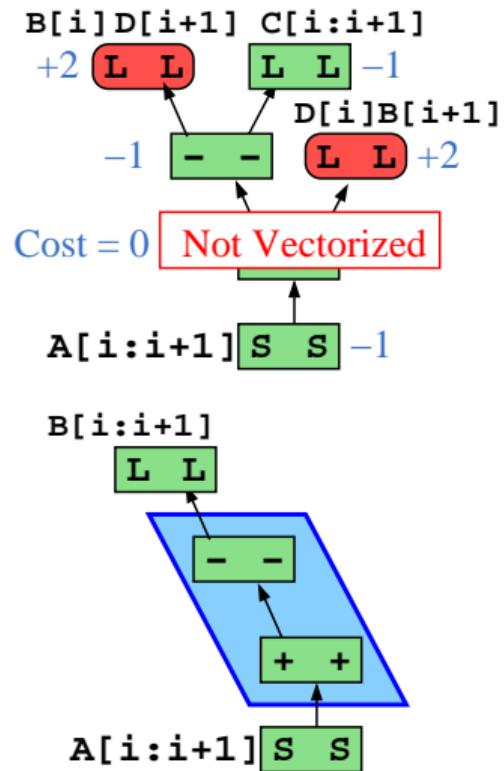
LSLP fails in the presence of inverse elements

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long A[],B[],C[],D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```



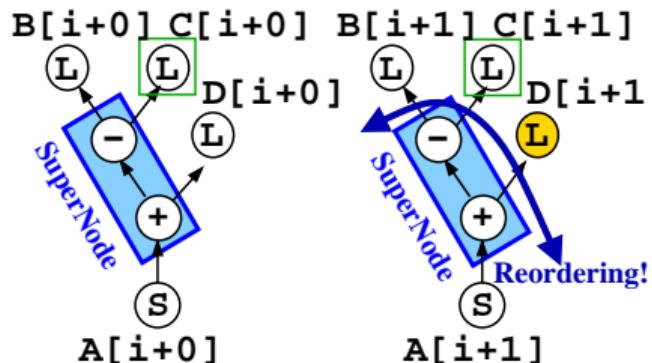
(L) SLP

SN-SLP



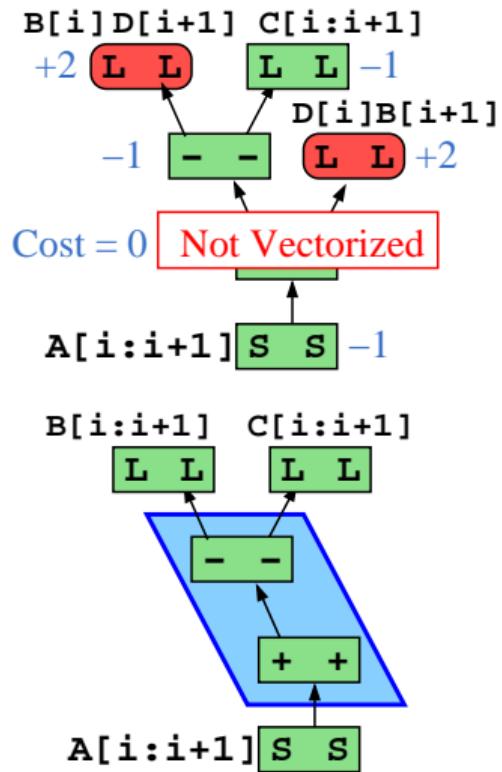
LSLP fails in the presence of inverse elements

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A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```



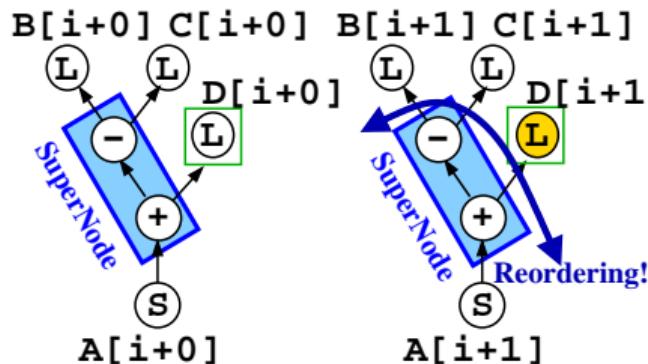
(L) SLP

SN-SLP



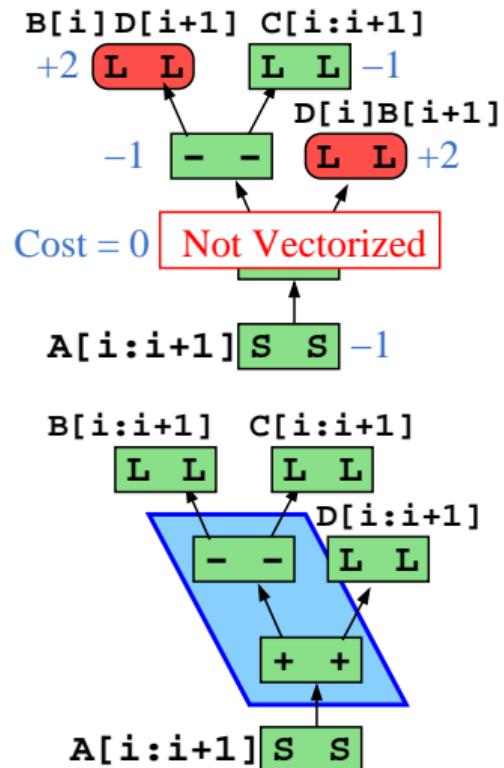
LSLP fails in the presence of inverse elements

```
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A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```



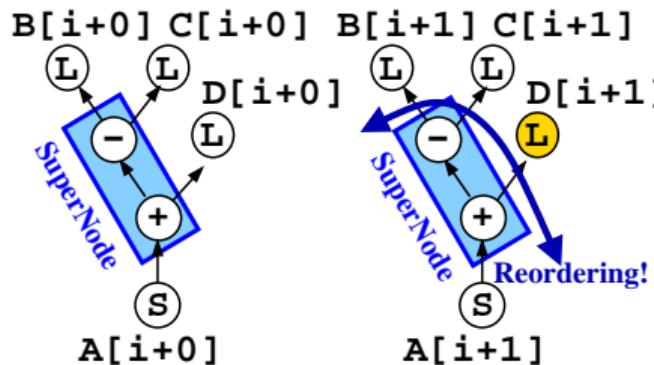
(L) SLP

SN-SLP



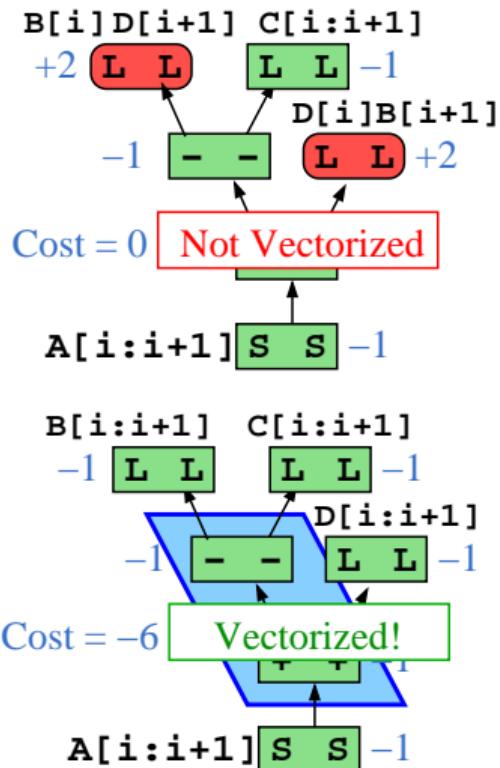
LSLP fails in the presence of inverse elements

```
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A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=D[i+1]-C[i+1]+B[i+1];
```



(L) SLP

SN-SLP

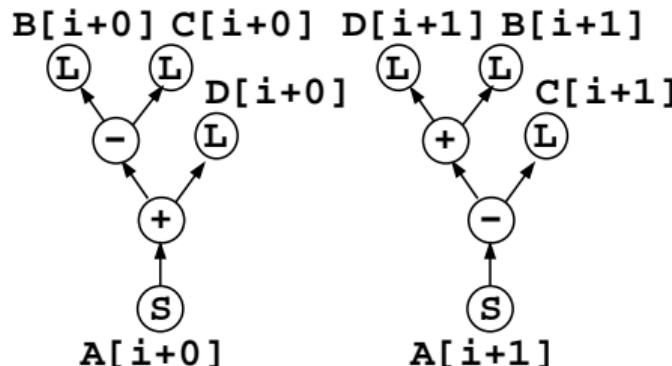


SuperNode internal nodes can be reordered too

```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```

SuperNode internal nodes can be reordered too

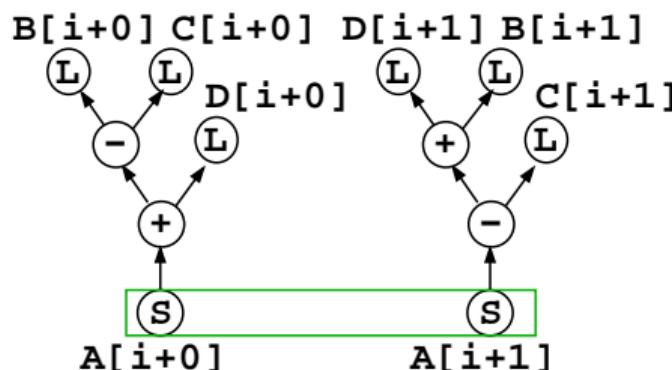
```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```



SuperNode internal nodes can be reordered too

```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```

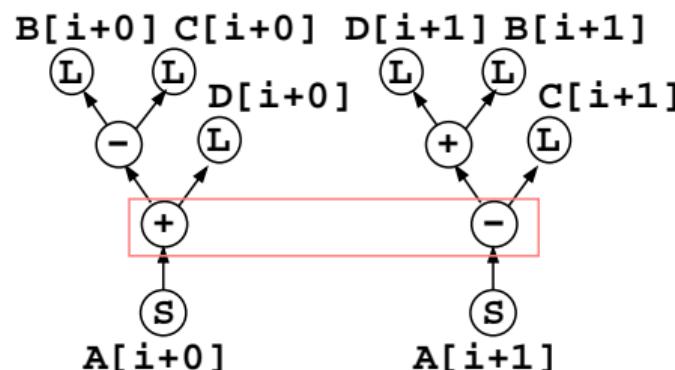
(L) SLP



A[i:i+1] [S S]

SuperNode internal nodes can be reordered too

```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```

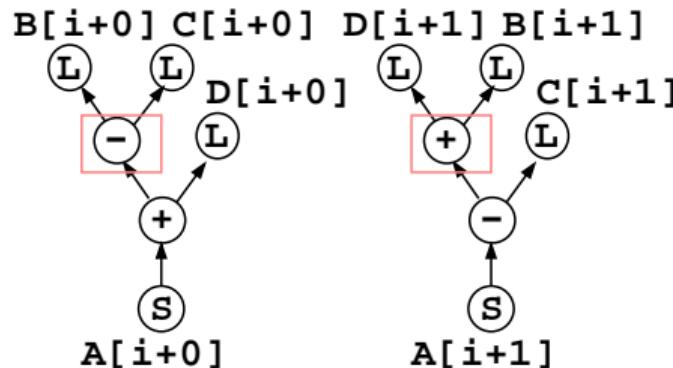


(T) SLP

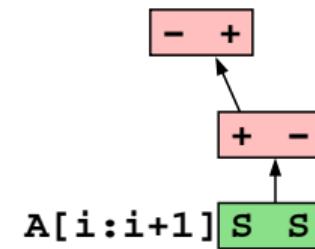


SuperNode internal nodes can be reordered too

```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```

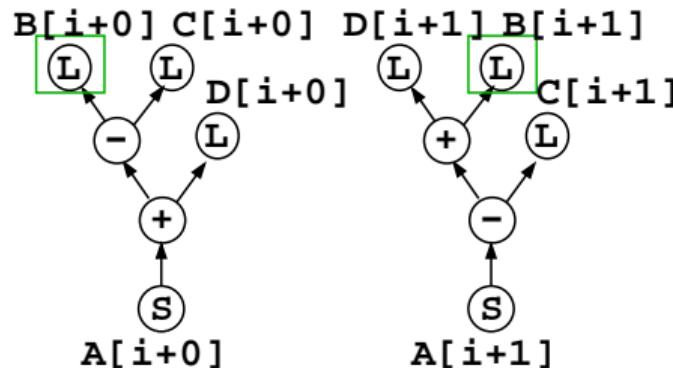


(I) SLP

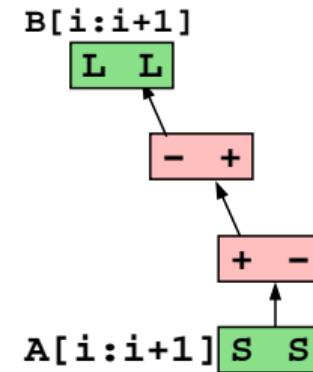


SuperNode internal nodes can be reordered too

```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```

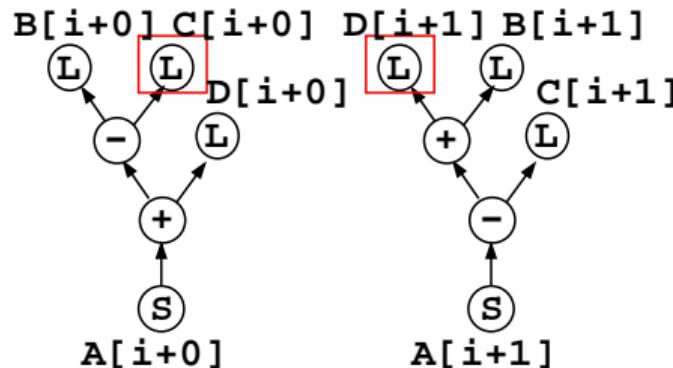


(I) SLP

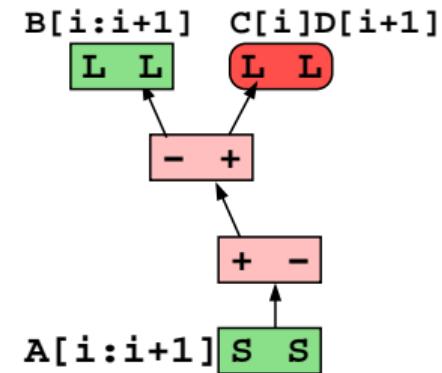


SuperNode internal nodes can be reordered too

```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```

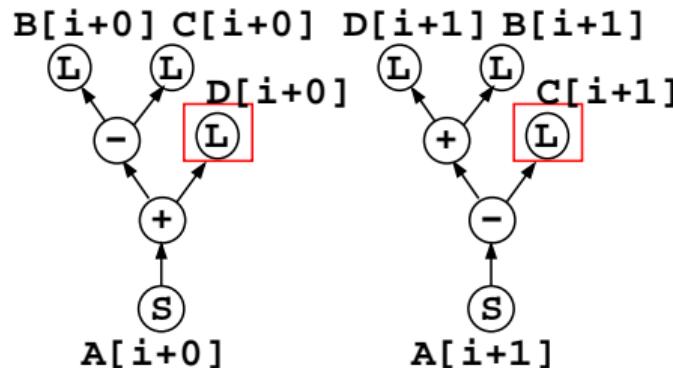


(π) SLP

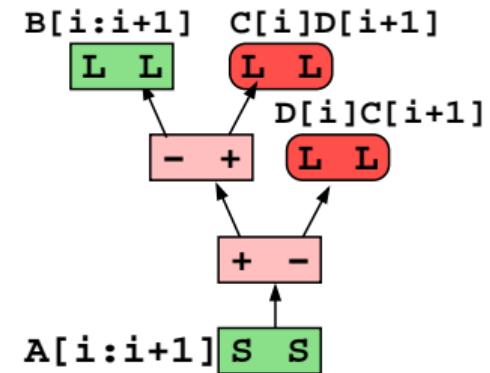


SuperNode internal nodes can be reordered too

```
long A[],B[],C[],D[];  
A[i+0]=B[i+0]-C[i+0]+D[i+0];  
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```

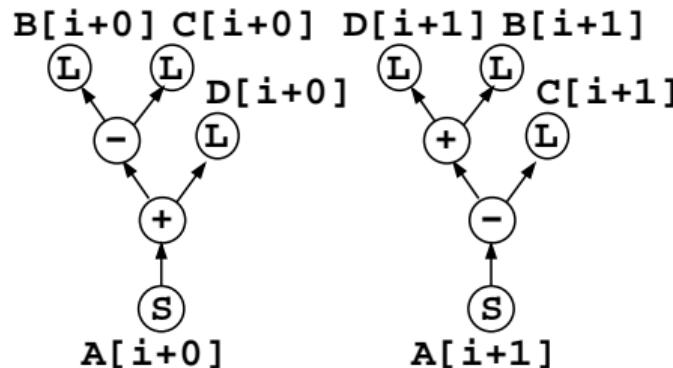


(π) SLP

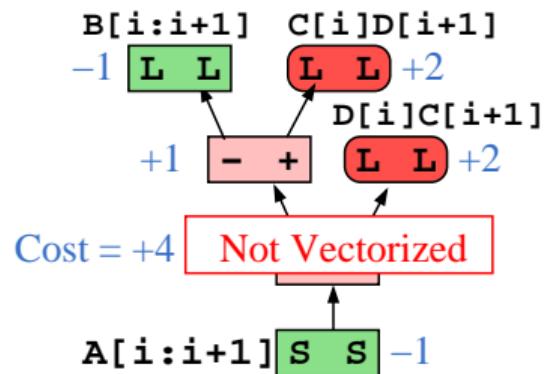


SuperNode internal nodes can be reordered too

```
long A[], B[], C[], D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```

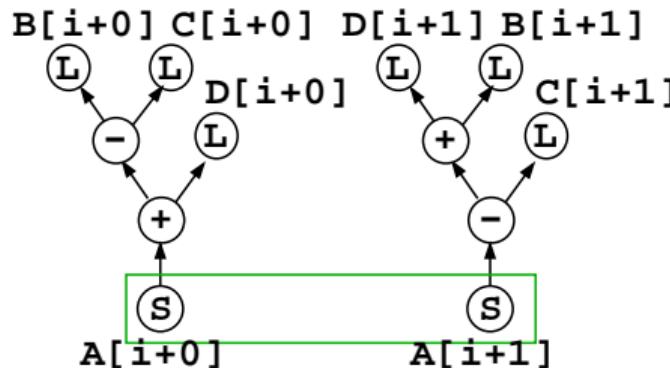


(I) SLP

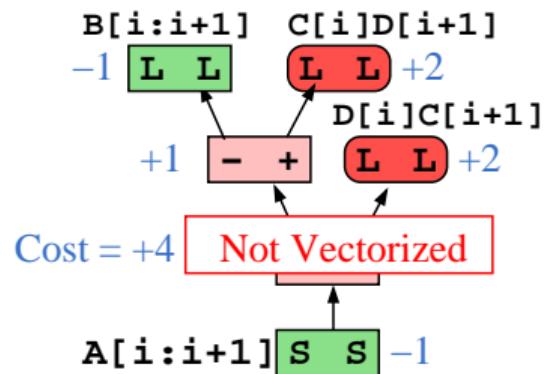


SuperNode internal nodes can be reordered too

```
long A[], B[], C[], D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```



(I) SLP

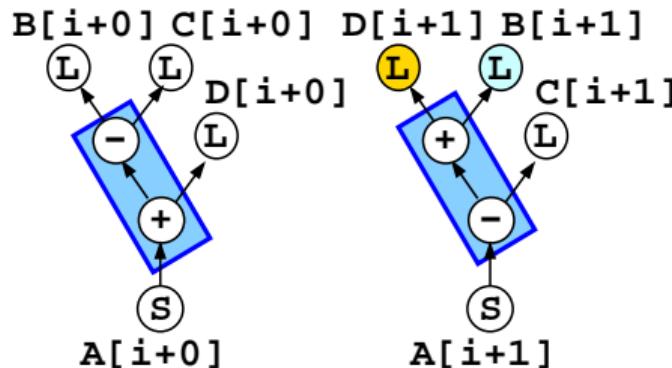


SN-SLP

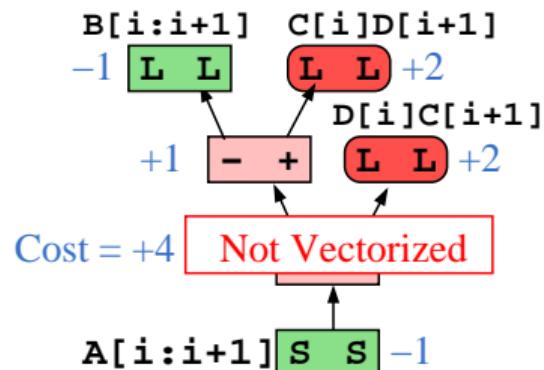
A[i:i+1] S S

SuperNode internal nodes can be reordered too

```
long A[],B[],C[],D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```



(I) SLP

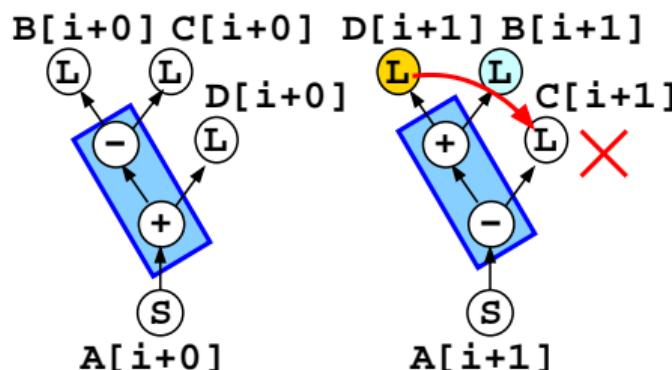


SN-SLP

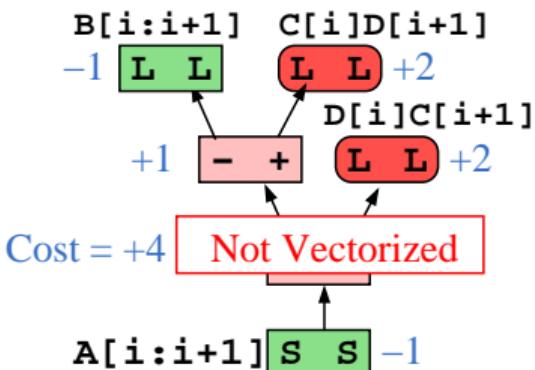
$A[i:i+1] [S \ S]$

SuperNode internal nodes can be reordered too

```
long A[], B[], C[], D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```



(I) SLP

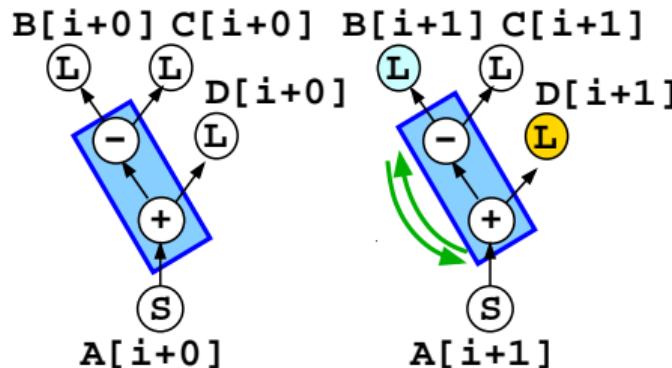


SN-SLP

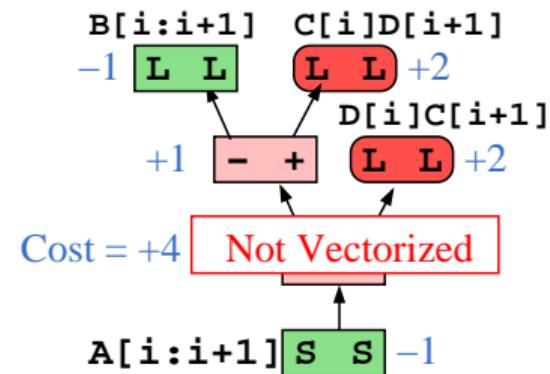
$A[i:i+1]$ (S S)

SuperNode internal nodes can be reordered too

```
long A[], B[], C[], D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```



(I) SLP

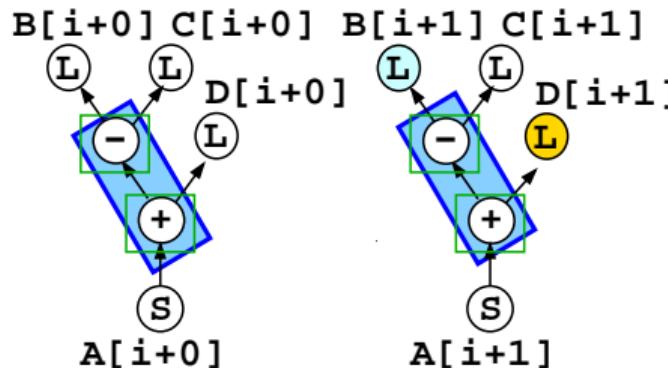


SN-SLP

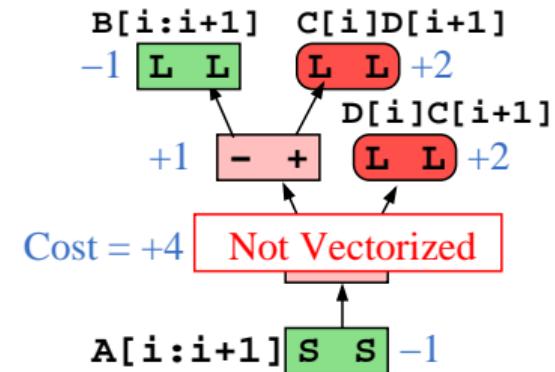
$A[i:i+1] [S \ S]$

SuperNode internal nodes can be reordered too

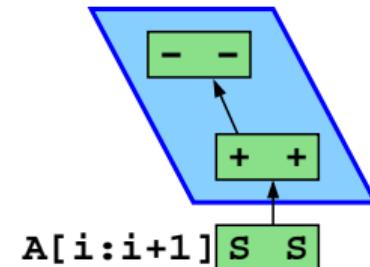
```
long A[],B[],C[],D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```



(I) SLP

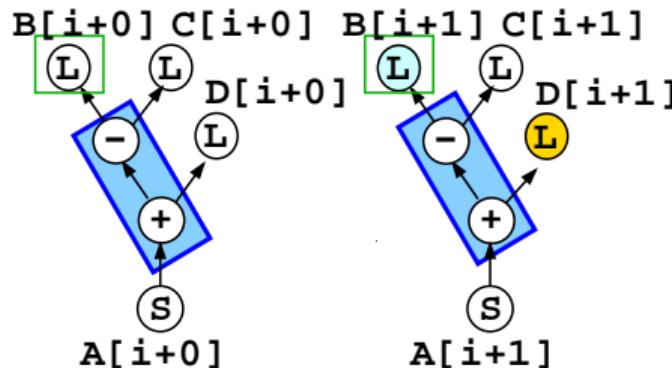


SN-SLP



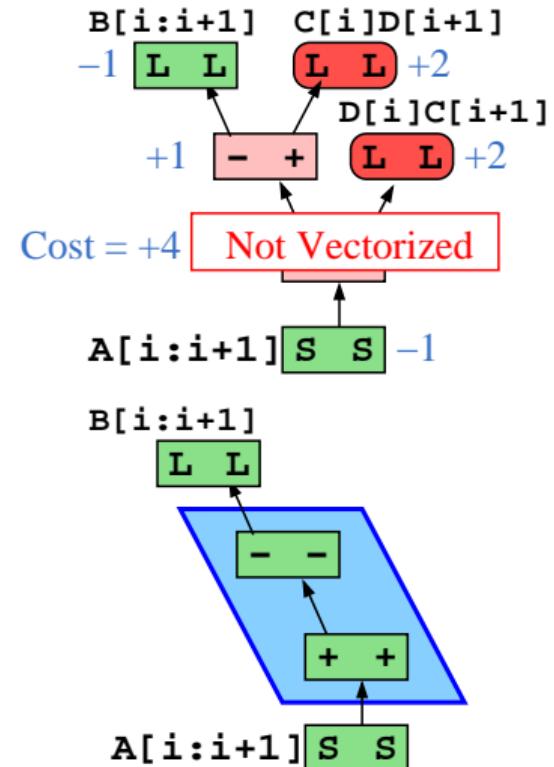
SuperNode internal nodes can be reordered too

```
long A[],B[],C[],D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```



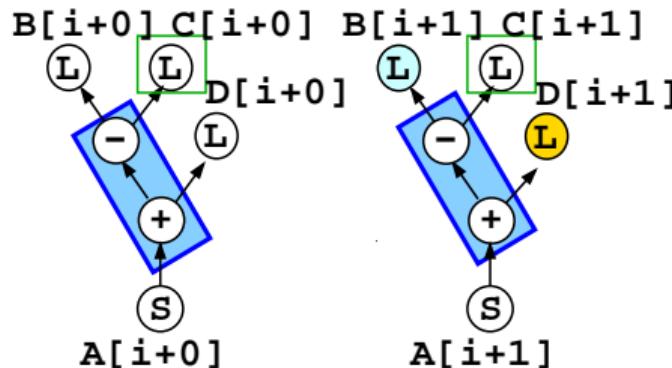
(Σ) SLP

SN-SLP



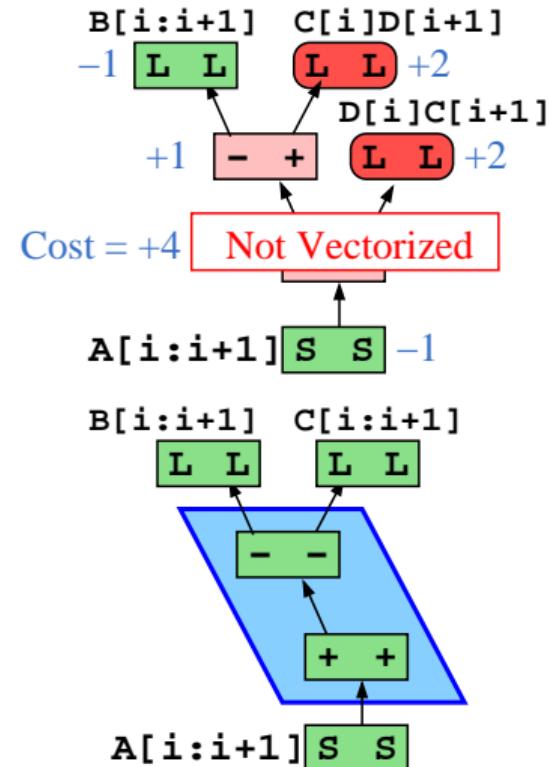
SuperNode internal nodes can be reordered too

```
long A[],B[],C[],D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```



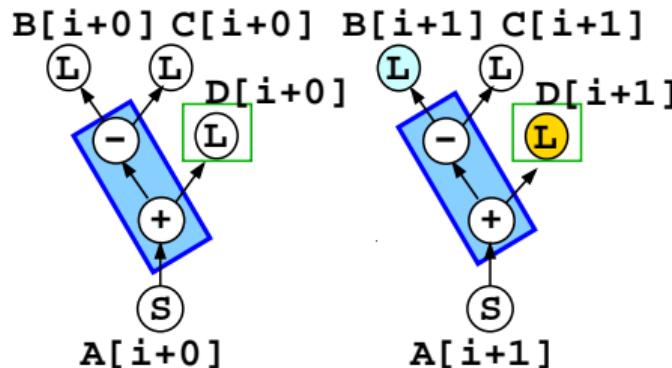
(L) SLP

SN-SLP



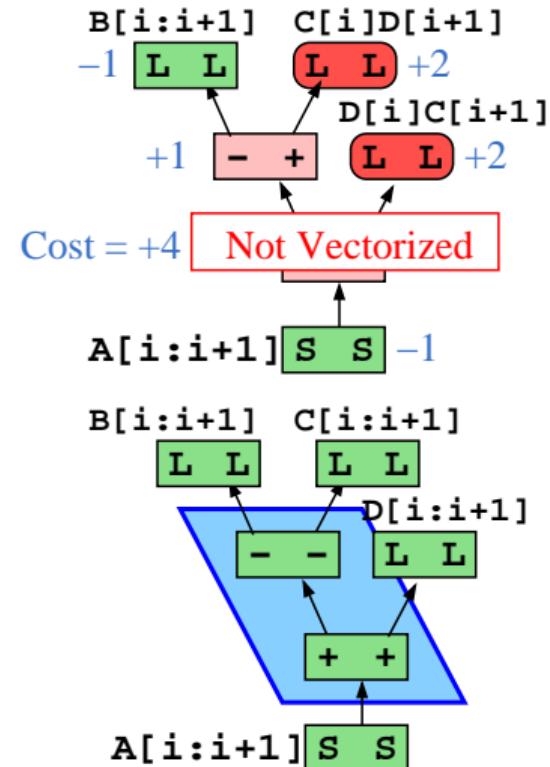
SuperNode internal nodes can be reordered too

```
long A[],B[],C[],D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```



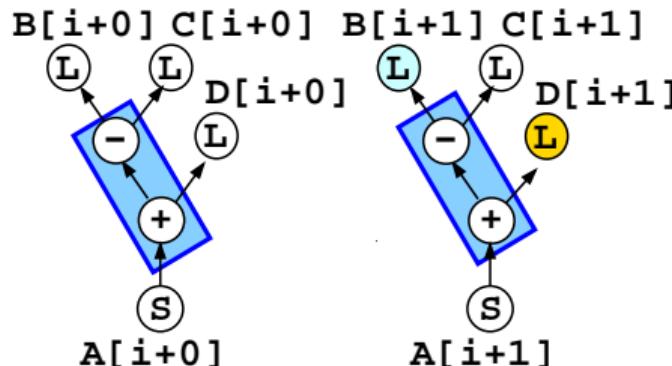
(I) SLP

SN-SLP



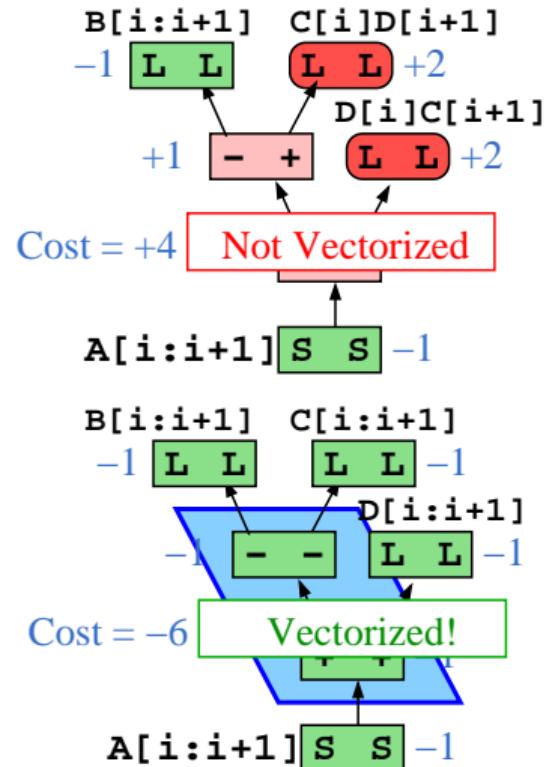
SuperNode internal nodes can be reordered too

```
long A[],B[],C[],D[];
A[i+0]=B[i+0]-C[i+0]+D[i+0];
A[i+1]=B[i+1]+D[i+1]-C[i+1];
```

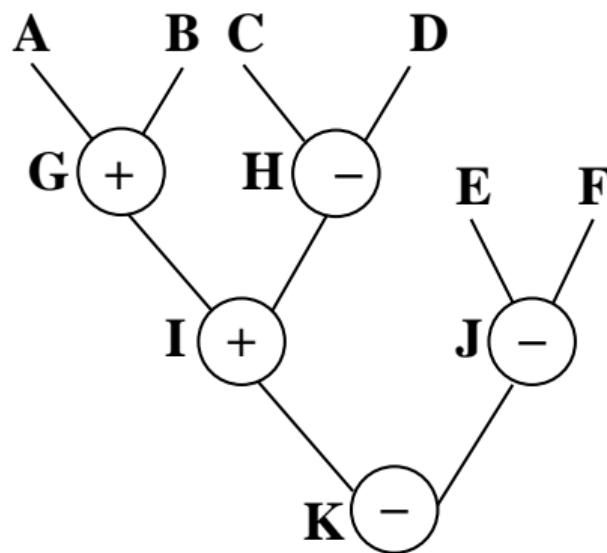


(Σ) SLP

SN-SLP

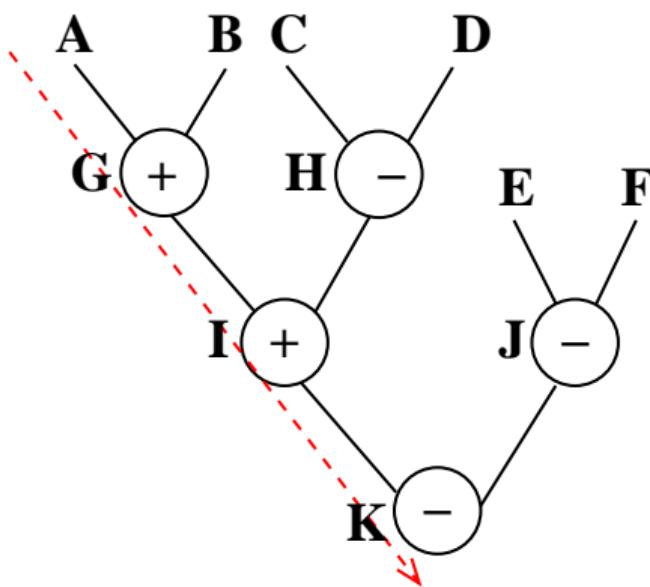


Legality



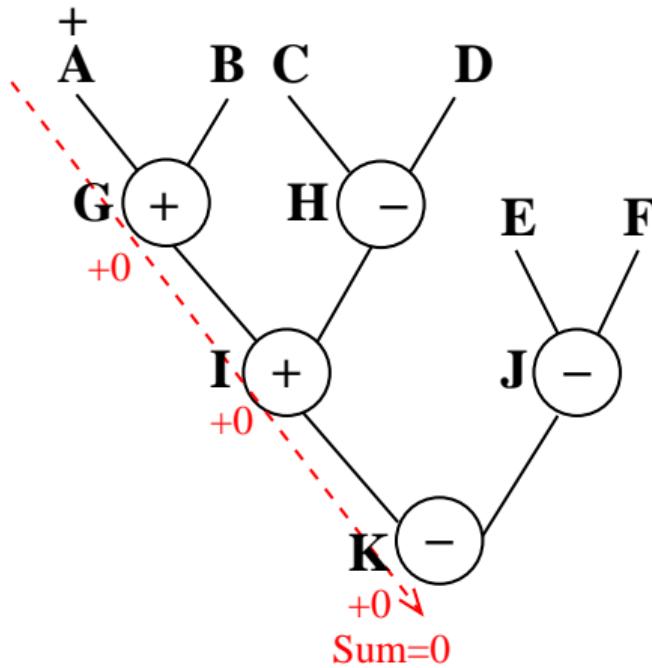
Accumulated Path Operation (APO)	Linearized

Legality



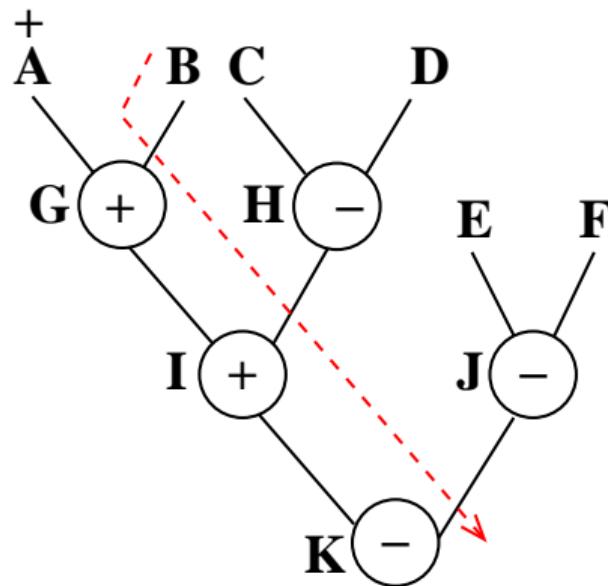
Accumulated Path Operation (APO)	Linearized

Legality



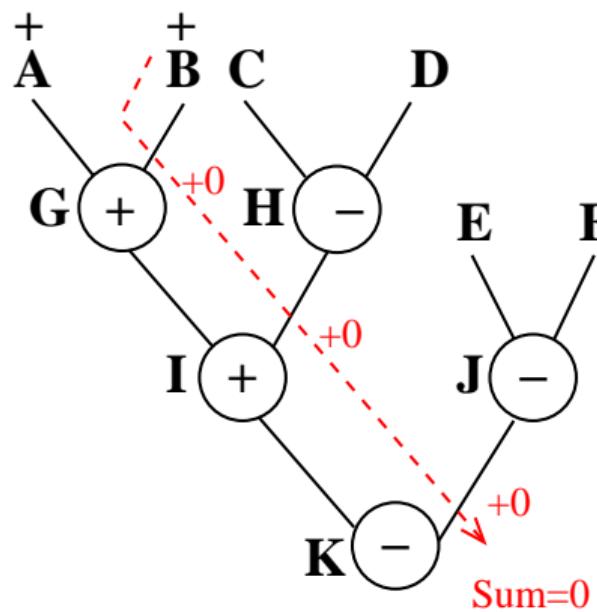
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	+ A

Legality



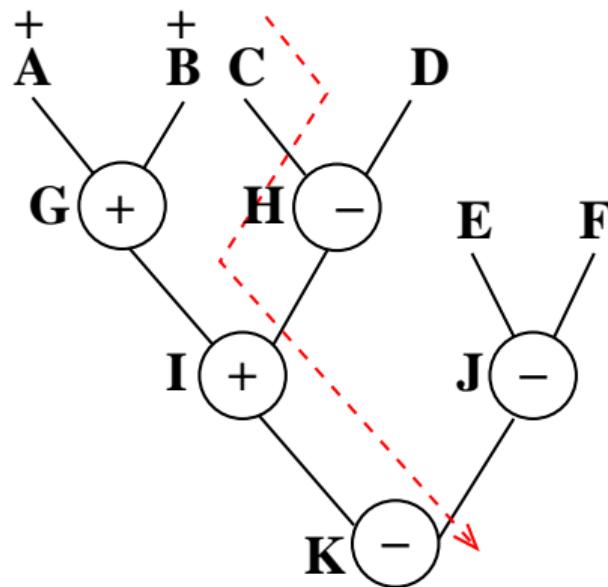
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	+ A

Legality



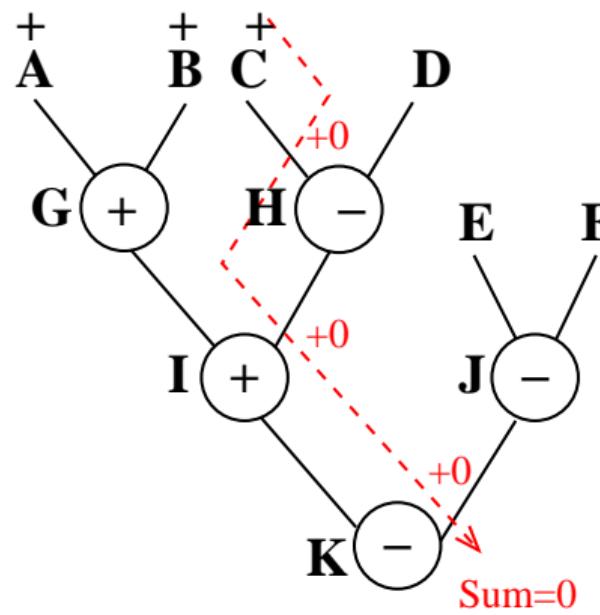
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A + B
B	0	+	

Legality



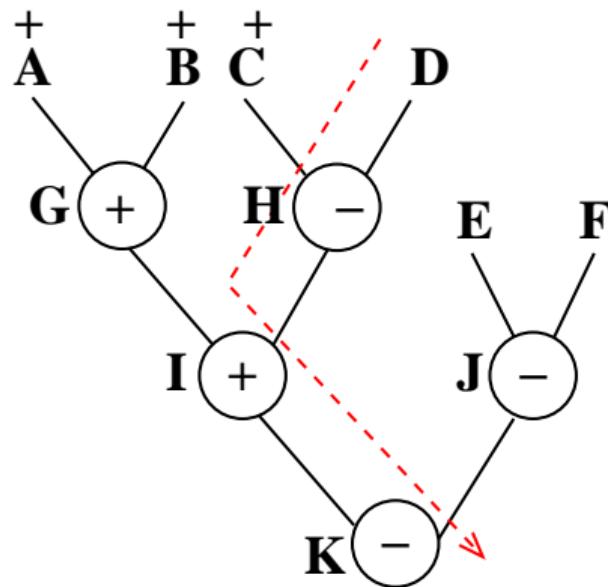
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A + ↓ B
B	0	+	

Legality



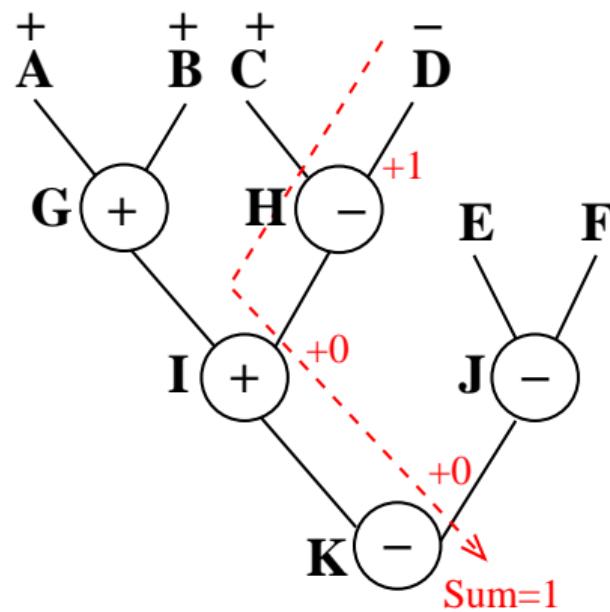
	Accumulated Path Operation (APO)	Linearized
A	0 +	A
B	0 +	B
C	0 +	C

Legality



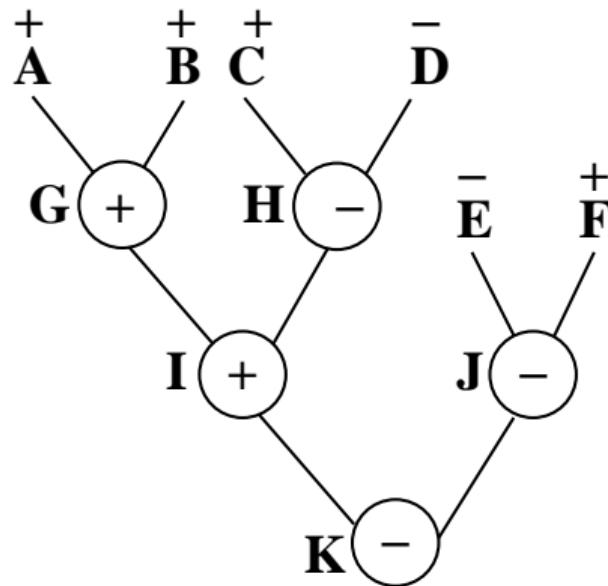
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A ↓ B ↓ C
B	0	+	
C	0	+	

Legality



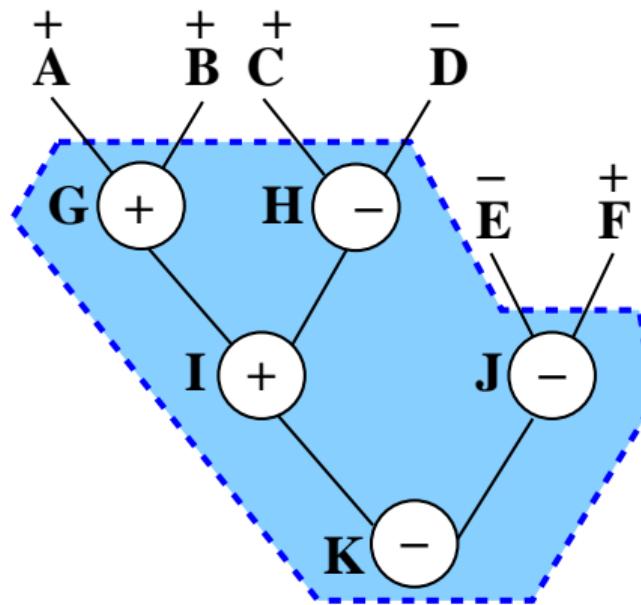
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A
B	0	+	↓ B
C	0	+	↓ C
D	1	-	↓ D

Legality



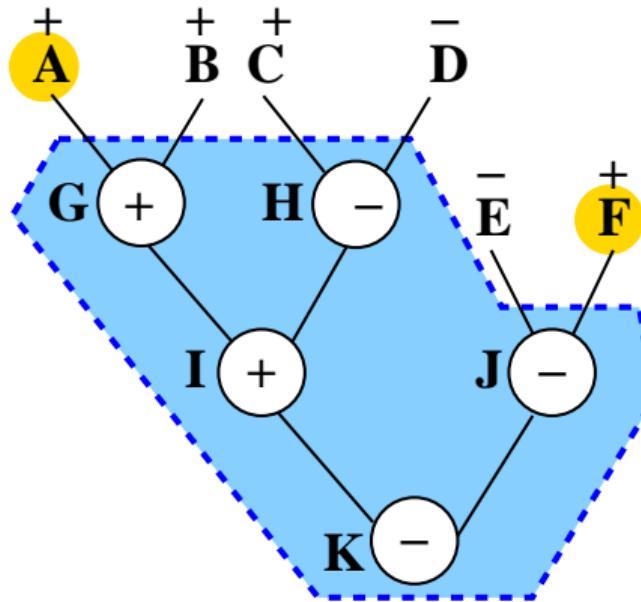
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A
B	0	+	↓ B
C	0	+	↓ C
D	1	-	↓ D
E	1	-	↓ E
F	2	+	↓ F
G	0	+	↓ G
H	0	+	↓ H
I	0	+	↓ I
J	1	-	↓ J
K	0	+	↓ K

Legality



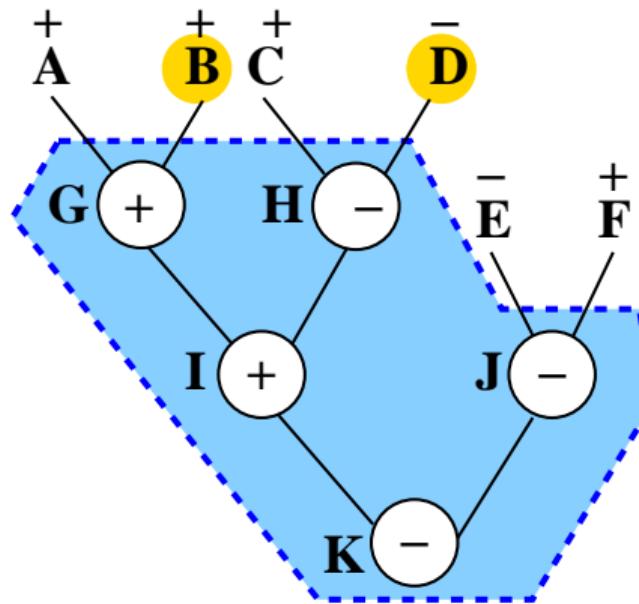
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A
B	0	+	↓ B
C	0	+	↓ C
D	1	-	↓ D
E	1	-	↓ E
F	2	+	↓ F
G	0	+	↓ G
H	0	+	↓ H
I	0	+	↓ I
J	1	-	↓ J
K	0	+	↓ K

Legality



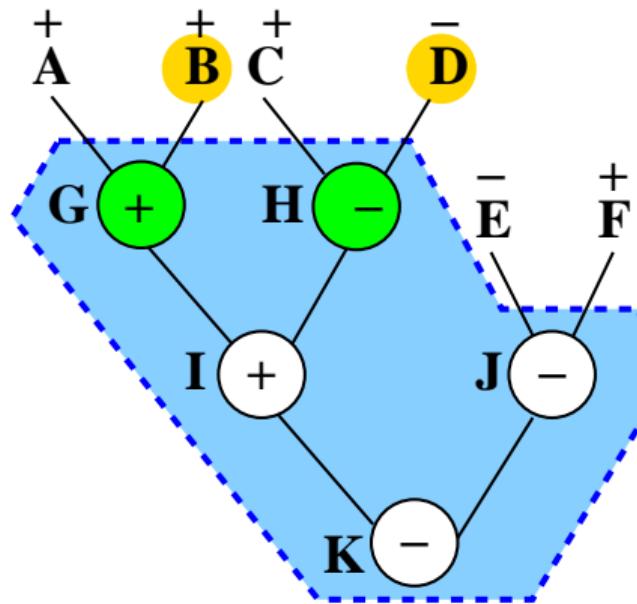
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A
B	0	+	↓ B
C	0	+	↓ C
D	1	-	↓ D
E	1	-	↓ E
F	2	+	↓ F
G	0	+	↓ G
H	0	+	↓ H
I	0	+	↓ I
J	1	-	↓ J
K	0	+	↓ K

Legality



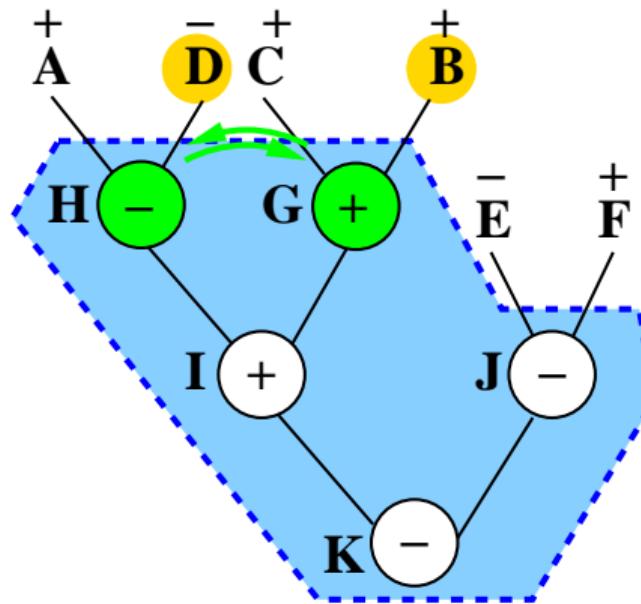
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A
B	0	+	+ B
C	0	+	+ C
D	1	-	+ D
E	1	-	- E
F	2	+	- F
G	0	+	+ G
H	0	+	+ H
I	0	+	+ I
J	1	-	- J
K	0	+	+ K

Legality



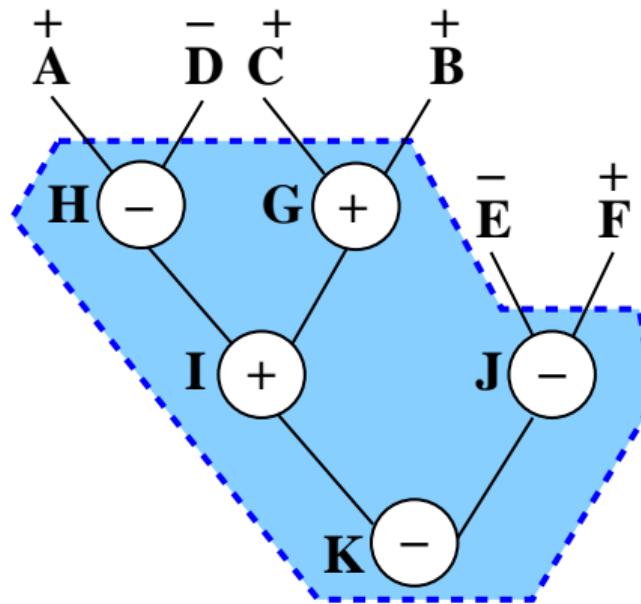
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A
B	0	+	+ B
C	0	+	+ C
D	1	-	- D
E	1	-	- E
F	2	+	+ F
G	0	+	+ G
H	0	+	+ H
I	0	+	+ I
J	1	-	- J
K	0	+	+ K

Legality



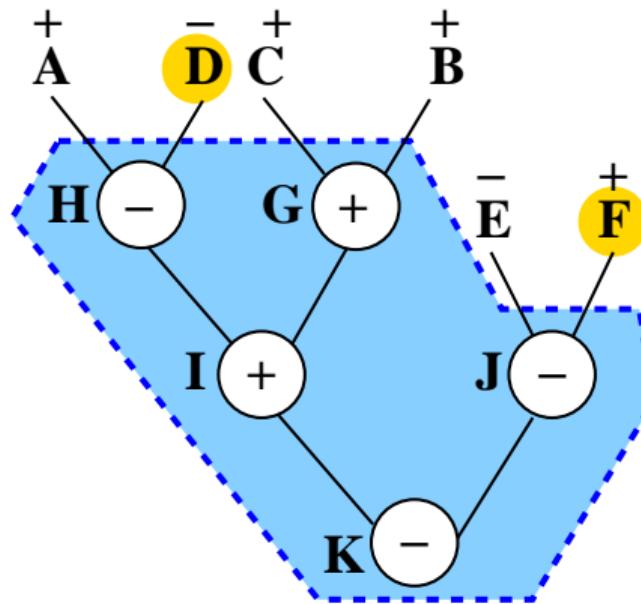
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A
B	0	+	+ B
C	0	+	+ C
D	1	-	+ D
E	1	-	- E
F	2	+	- F
G	0	+	+ G
H	0	+	+ H
I	0	+	+ I
J	1	-	- J
K	0	+	+ K

Legality



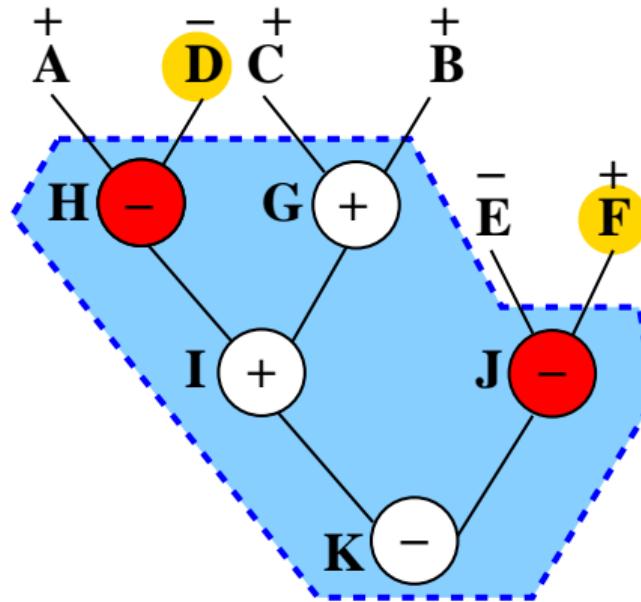
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A
B	0	+	↓ B
C	0	+	↓ C
D	1	-	↓ D
E	1	-	↓ E
F	2	+	↓ F
G	0	+	↓ G
H	0	+	↓ H
I	0	+	↓ I
J	1	-	↓ J
K	0	+	↓ K

Legality



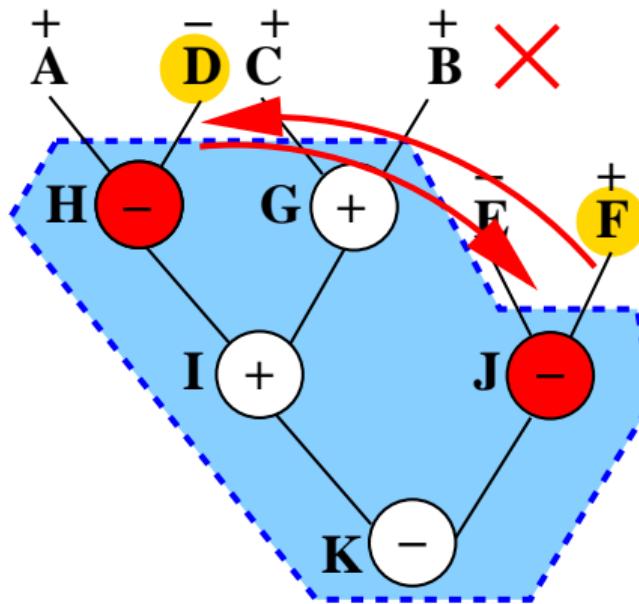
	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A
B	0	+	↓ B
C	0	+	↓ C
D	1	-	↓ D
E	1	-	↓ E
F	2	+	↓ F
G	0	+	↓ G
H	0	+	↓ H
I	0	+	↓ I
J	1	-	↓ J
K	0	+	↓ K

Legality



	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A
B	0	+	↓ B
C	0	+	↓ C
D	1	-	↓ D
E	1	-	↓ E
F	2	+	↓ F
G	0	+	↓ G
H		+	↓ H
I	0	+	↓ I
J	0	-	↓ J
K	0	+	↓ K

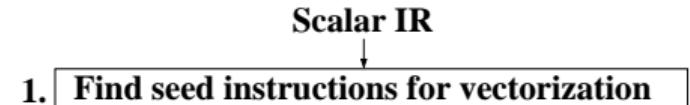
Legality



	Sum	Accumulated Path Operation (APO)	Linearized
A	0	+	A
B	0	+	+ B
C	0	+	+ C
D	1	-	+ - D
E	1	-	+ - E
F	2	+	+ - + F
G	0	+	+ + G
H		+	+ + + H
I	0	+	+ + + I
J	0	-	+ + - J
K	0	+	+ + + K

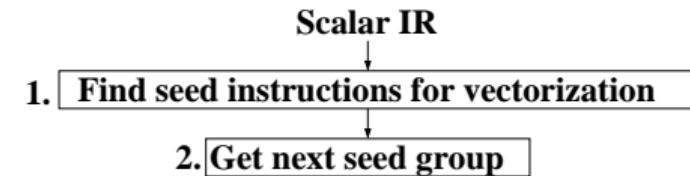
SN-SLP Algorithm

- Seed instructions are usually:
 - ① Consecutive Stores
 - ② Reductions



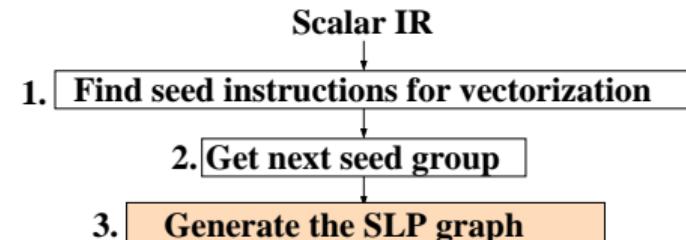
SN-SLP Algorithm

- Seed instructions are usually:
 - ① Consecutive Stores
 - ② Reductions



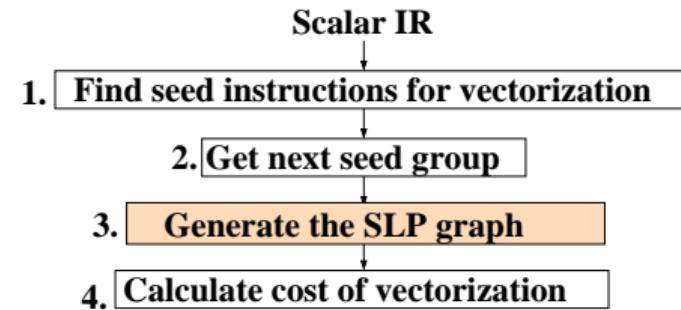
SN-SLP Algorithm

- Seed instructions are usually:
 - ① Consecutive Stores
 - ② Reductions
- Graph contains groups of vectorizable instructions



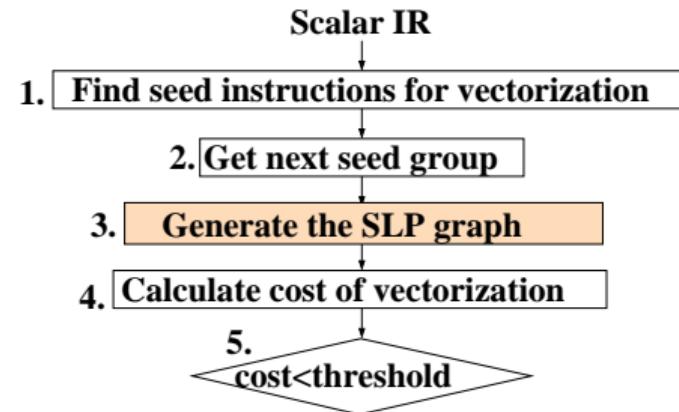
SN-SLP Algorithm

- Seed instructions are usually:
 - ① Consecutive Stores
 - ② Reductions
- Graph contains groups of vectorizable instructions
- Cost: weighted instr. count (TTI)



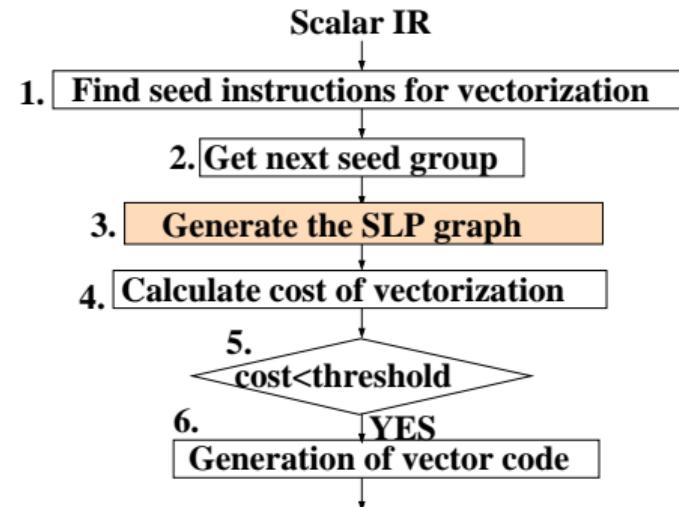
SN-SLP Algorithm

- Seed instructions are usually:
 - ① Consecutive Stores
 - ② Reductions
- Graph contains groups of vectorizable instructions
- Cost: weighted instr. count (TTI)
- Check overall profitability



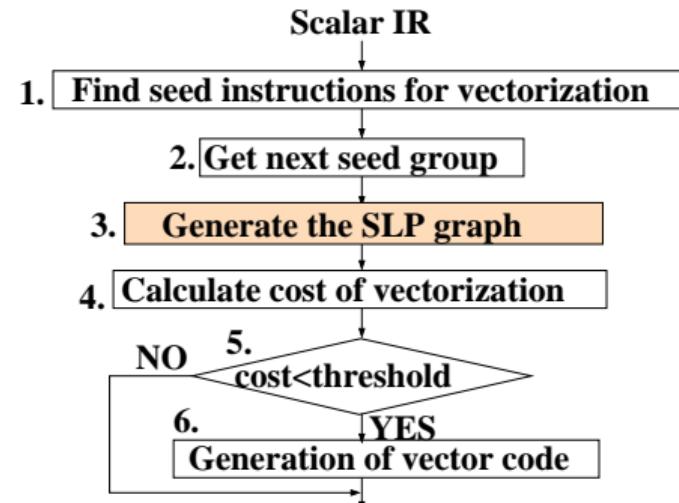
SN-SLP Algorithm

- Seed instructions are usually:
 - ① Consecutive Stores
 - ② Reductions
- Graph contains groups of vectorizable instructions
- Cost: weighted instr. count (TTI)
- Check overall profitability
- Generate vector code



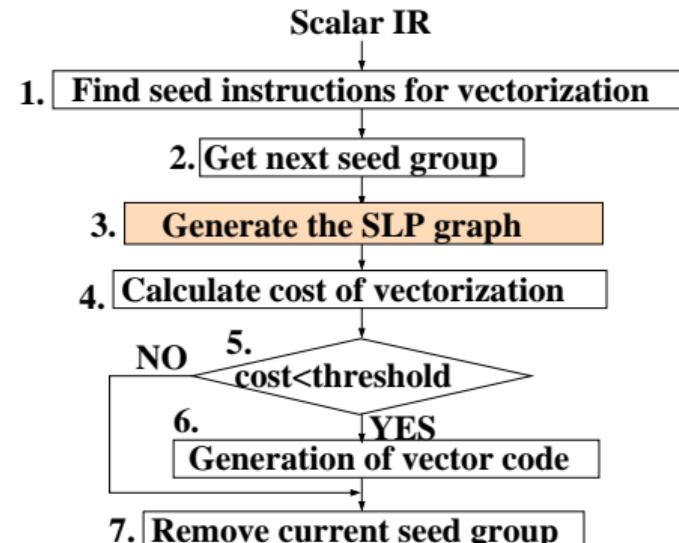
SN-SLP Algorithm

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- Graph contains groups of vectorizable instructions
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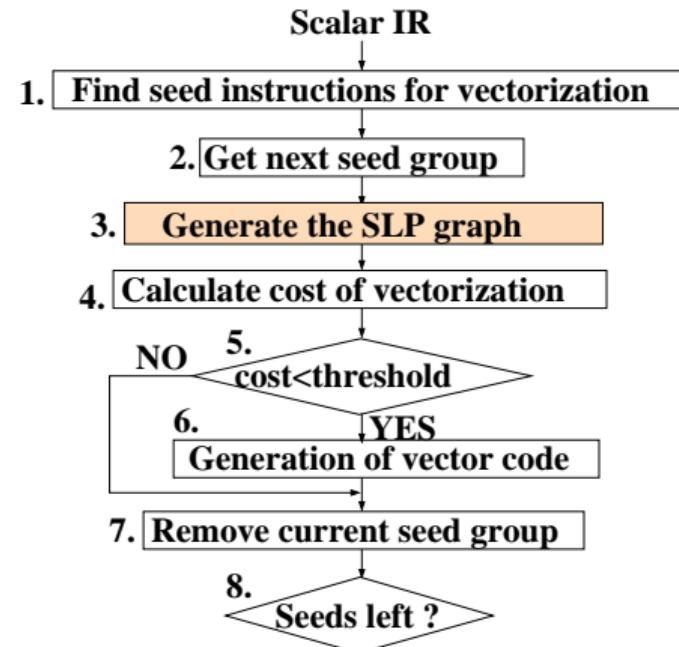
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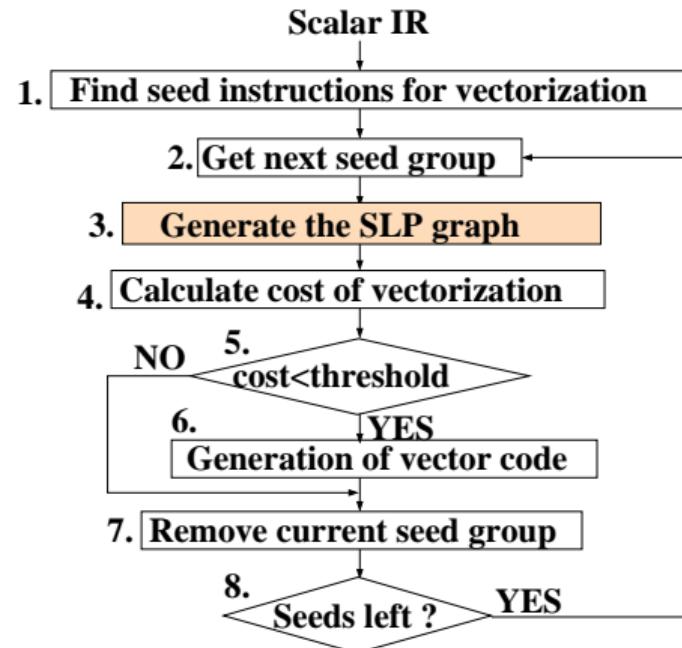
SN-SLP Algorithm

- Seed instructions are usually:
 - ① Consecutive Stores
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- Graph contains groups of vectorizable instructions
- Cost: weighted instr. count (TTI)
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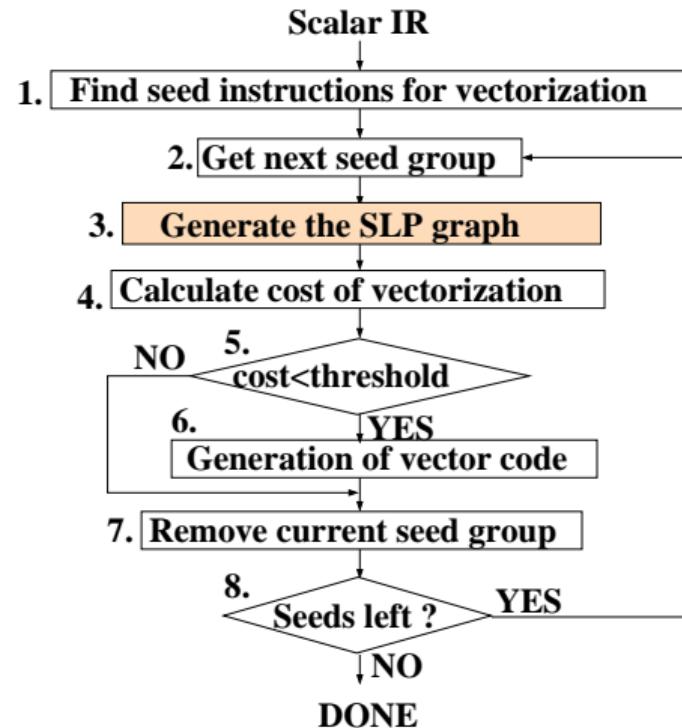
SN-SLP Algorithm

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 - ① Consecutive Stores
 - ② Reductions
- Graph contains groups of vectorizable instructions
- Cost: weighted instr. count (TTI)
- Check overall profitability
- Generate vector code
- Repeat



SN-SLP Algorithm

- Seed instructions are usually:
 - ① Consecutive Stores
 - ② Reductions
- Graph contains groups of vectorizable instructions
- Cost: weighted instr. count (TTI)
- Check overall profitability
- Generate vector code
- Repeat



Experimental Setup

- Implemented in LLVM trunk

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- Target: Intel® Core™ i5-6440HQ CPU

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- Implemented in LLVM trunk
- Target: Intel® Core™ i5-6440HQ CPU
- Compiler flags: -O3 -ffast-math -march=native -mtune=native

Experimental Setup

- Implemented in LLVM trunk
- Target: Intel® Core™ i5-6440HQ CPU
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- Kernels from unmodified functions of SPEC CPU2006

Experimental Setup

- Implemented in LLVM trunk
- Target: Intel® Core™ i5-6440HQ CPU
- Compiler flags: -O3 -ffast-math -march=native -mtune=native
- Kernels from unmodified functions of SPEC CPU2006
- We evaluated the following:

Experimental Setup

- Implemented in LLVM trunk
- Target: Intel® Core™ i5-6440HQ CPU
- Compiler flags: -O3 -ffast-math -march=native -mtune=native
- Kernels from unmodified functions of SPEC CPU2006
- We evaluated the following:
 - ① O3 : All vectorizers disabled

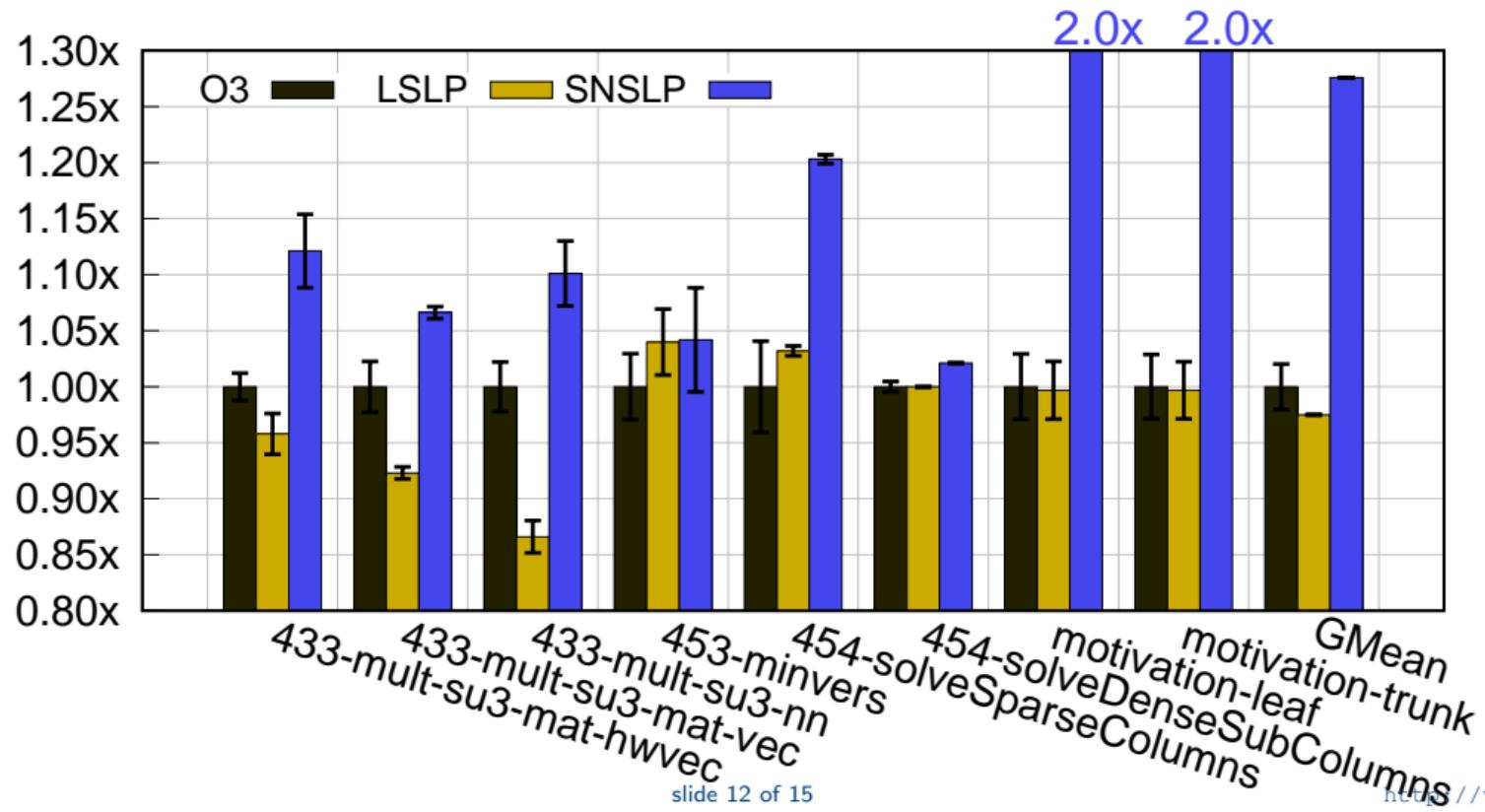
Experimental Setup

- Implemented in LLVM trunk
- Target: Intel® Core™ i5-6440HQ CPU
- Compiler flags: -O3 -ffast-math -march=native -mtune=native
- Kernels from unmodified functions of SPEC CPU2006
- We evaluated the following:
 - ① O3 : All vectorizers disabled
 - ② LSLP : O3 + LSLP

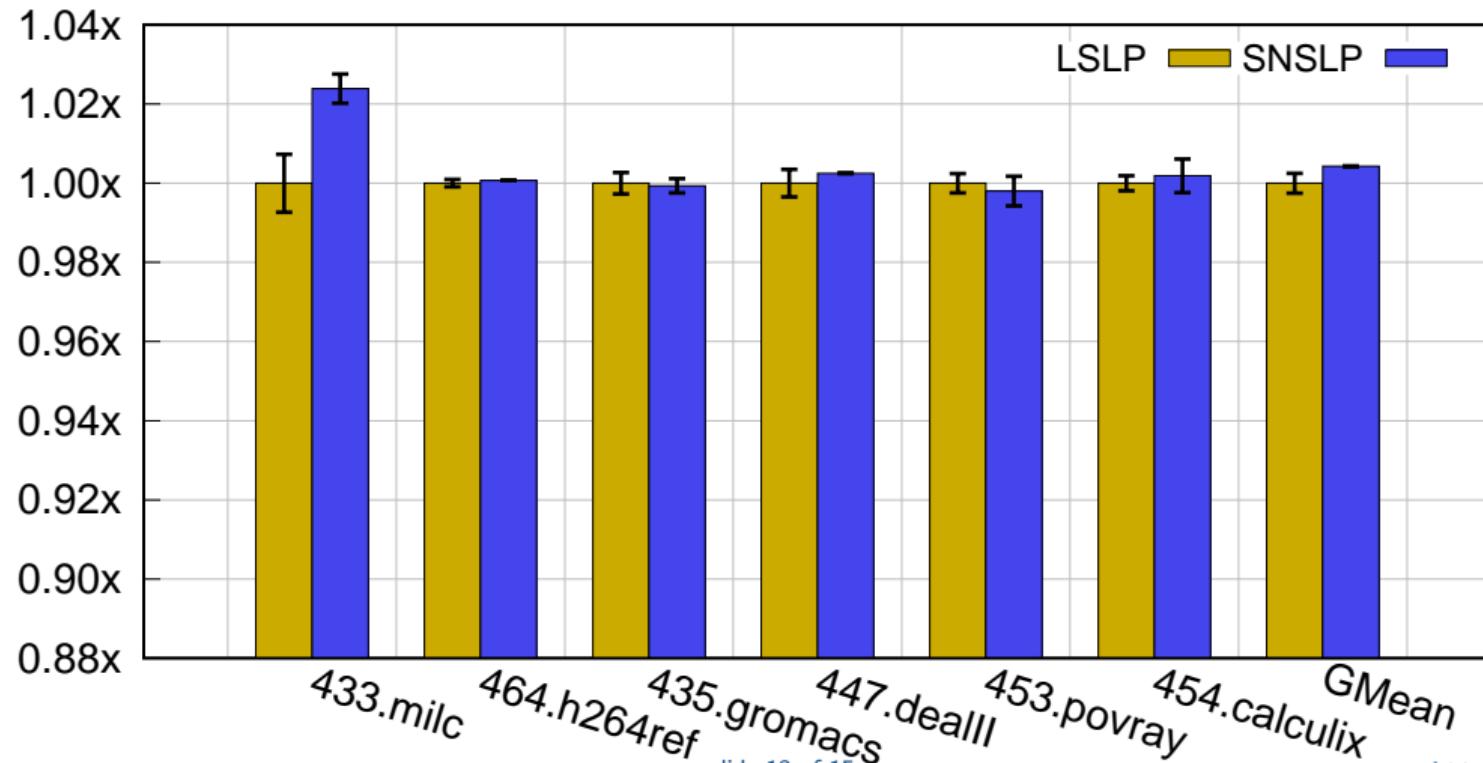
Experimental Setup

- Implemented in LLVM trunk
- Target: Intel® Core™ i5-6440HQ CPU
- Compiler flags: -O3 -ffast-math -march=native -mtune=native
- Kernels from unmodified functions of SPEC CPU2006
- We evaluated the following:
 - ① O3 : All vectorizers disabled
 - ② LSLP : O3 + LSLP
 - ③ SNSLP : O3 + SN-SLP

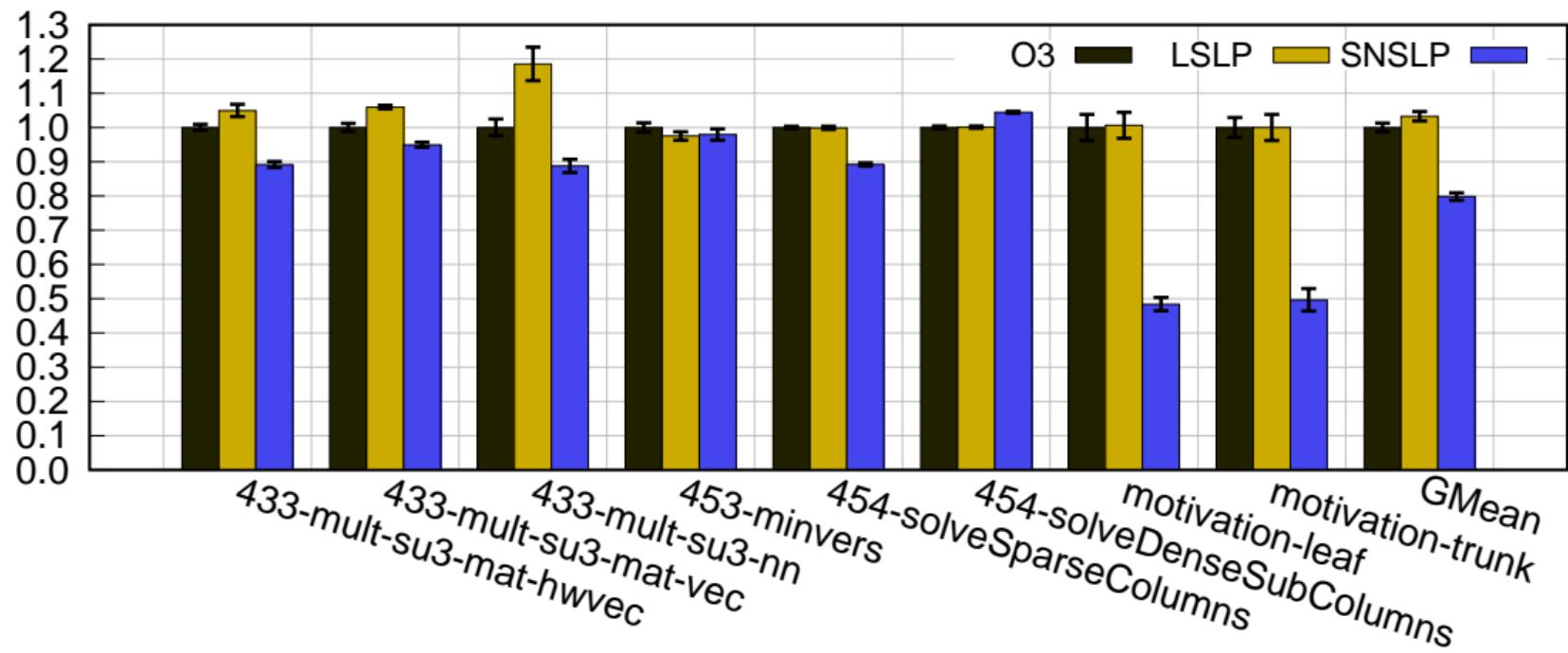
Performance of kernels



Performance (Full Benchmarks)



Total Compilation Time



Conclusion

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- Improves performance with similar compilation time